

Cryptography: Basics & Applications

2013 JMU Cyber Defense Boot Camp

What is this unit about?

- Lecturing
 - “**Boring**” lecturing (practice in next session)
- A topic that has challenged the human kind for more than 2000 years
 - Dated beyond Julius Caesar (around 56 BC)
- Slides are available at
<https://users.cs.jmu.edu/tjadenbc/Bootcamp/3-crypto.pdf>



Organization

- The data confidentiality problem
- Theory
 - Numbers
 - Encryption
 - Digital signature
 - Cryptographic hashing
 - Digital certificates and PKI
- Tie everything together: HTTPS

Focus on **concepts**;

Skip **details**

Road Map

- The data confidentiality problem
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Questions

- How do you protect (the **confidentiality** of) your **Turbo Tax** file on your computer?
 - Full name, SSN, DOB, home address
- How do you protect the financial information on your computer?
 - Bank accounts, retirement plan accounts, stock investment accounts

Encrypt them?

What is encryption?

What the heck is Cryptography?

- We have heard “encryption” more
- Cryptography
 - Kryptos: hidden
 - -graphy
 - writing or representation in a (specified) manner or by a (specified) means or of a (specified) object
- Traditionally, cryptography = encryption

Welcome to the Wonderful Land

- **Q:** How many cryptographers does it take to change a light bulb?
- **A:** XIGHCBS

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Road Map

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Warm-up Questions

- $2^3 = ?$
- $2^4 = ?$
- $2^3 < 10 < 2^4 ?$
- $\log_2 8 = ?$
- $\log_2 16 = ?$
- $\log_2 10 = ?$
- $\log_2(10^6) = ?$
- $\log_2(10^9) = ?$

Back-of-Envelope Calculations

- How many seconds are there in a day?

$$24 \times 60 \times 60 = 86,400 \text{ seconds}$$

In 2^x ?

$$\leq 2^{17}$$

How?

$$86400 = 2^x$$

$$8 \times 10^4 \approx 2^x$$

$$\log_2(8 \times 10^4) \approx \log_2(2^x)$$

$$\log_2 8 + \log_2(10^4) \approx x$$

$$3 + 4 \times \log_2(10) \approx x$$

$$x \approx 16.3$$

Back-of-Envelope Calculations

- How many seconds are there in a day?

$$24 \times 60 \times 60 = 86,400 \text{ seconds}$$

$$\ln 2^x?$$

$$\leq 2^{17}$$

$$100 \text{ years} \approx 2^{32} \text{ seconds}$$

- How many seconds are there in a year?

$$365 \text{ days} \times 86,400 = 31,536,000$$

$$\leq 2^{25}$$

- How many seconds in 100 years?

$$3,153,600,000 \text{ seconds} = 3.1536 \times 10^9$$

$$\approx 3.1536 \times 2^{30} \leq 2^{32}$$

Seconds in $2^?$

- 1 hour: $60 \times 60 = 3600$ seconds ($\leq 2^{12}$)
- 1 day: $24 \times 60 \times 60 = 86,400$ seconds ($\leq 2^{17}$)
- 1 month: $30 \text{ days} \times 86,400 = 2,592,000$ seconds ($< 2^{22}$)
- 1 year: $365 \text{ days} \times 86,400 = 31,536,000$ ($< 2^{25}$)
- 100 years: $3,153,600,000$ seconds $= 3.1536 \times 10^9 \approx 3.1536 \times 2^{30} \leq 2^{32}$

Back-of-Envelope Calculations

- How many “operations” can a computer do in one second?

Intel CPU

- Intel CPU: 3.45GHz
- $3.45 \times 10^9 \text{ Hz}$
- Clock rate: 3.45×10^9 times per second
- Assumption: 3.45×10^9 basic operations per second
 - ❖ $3.45 \times 10^9 < 2^{32}$;
- So in 100 years, this CPU can exhaust $2^{32} \times 2^{32} = 2^{64}$ basic operations

Nov. 14, 2012

- Fastest computer:
 - <http://www.top500.org/>
- DOE/SC/Oak Ridge National Laboratory
 - ❖ 17590.0 TFlop/s (17.59 PFLOPS)
 - $17.59 \times 10^{15} \approx 10^{16.24} \approx 2^{54}$ calculations per second
- 100 years $\approx 2^{32}$ seconds
- 100 year's calculations: $2^{54} \times 2^{32} = 2^{86}$

What if 1000000 Such Supercomputers?

- One supercomputer: $17.59 \times 10^{15} \approx 10^{16.24}$
- 1000000 (10^6) such computers
 - ✦ $10^{22.64}$ calculations per second
 - $\approx 2^{75.22}$
- 100 years: 2^{32} seconds
- 100 years' calculations = ?
 $2^{75.22} \times 2^{32} \leq 2^{108}$

What if 1 billion Such Supercomputers?

- One supercomputer: $17.59 \times 10^{15} \approx 10^{16.24} \approx 2^{54}$ calculations per second
- 10000000000 ($10^9 \approx 2^{29.9}$) such computers
 $2^{54} \times 2^{29.9} \approx 2^{84}$ calculations per second
- 100 years: 2^{32} seconds
- How many calculations in 100 years?
 $2^{84} \times 2^{32} \approx 2^{116}$

Lessons?

Computers have computing limits

① Numbers (Intel CPU)

- # of seconds in a day? 2^{17}
- # of seconds in a year? 2^{25}
- # of seconds in 100 years? 2^{32}
- Intel CPU (3.45GHz) in 100 years? 2^{64}
- 1 million Intel CPU (3.45GHz) in 100 years: 2^{86}
- 1 billion Intel CPU (3.45GHz) in 100 years: 2^{94}

① Numbers (The Fastest Computer)

- # of seconds in a **day?** 2^{17}
- # of seconds in a **year?** 2^{25}
- # of seconds in **100 years?** 2^{32}
- **The fastest computer** in 100 years? 2^{86}
- **1 million** fastest computers in 100 years: 2^{108}
- **1 billion** fastest computers in 100 years: 2^{116}

So?



- A 128-bit string 0110101010101...
 - Randomly generated



- **How many** tries does it take to guess it correctly?

- On average: 2^{127}

- How long will it take for these tries?

- One billion Intel CPU (3.45GHz)?

800 billion years

- One billion fastest computers?

200 thousand years

Space

- 1K bytes
- 1M bytes
- 1G bytes
- 1Tera bytes (TB)
- 1Peta bytes (PB)
- 1 exabyte (EB)
- 1 zettabyte (ZB)
- 1 yottabyte (YB)

- 2^{10}
- 2^{20}
- 2^{30}
- 2^{40}
- 2^{50}
- 2^{60}
- 2^{70}
- 2^{80}

4 terabytes = 2^{42}

120 PB (memory)
 $\approx 2^{57}$

NSA data center in Utah: 5
zettabytes (storage)

Passwords vs. a Strong Key

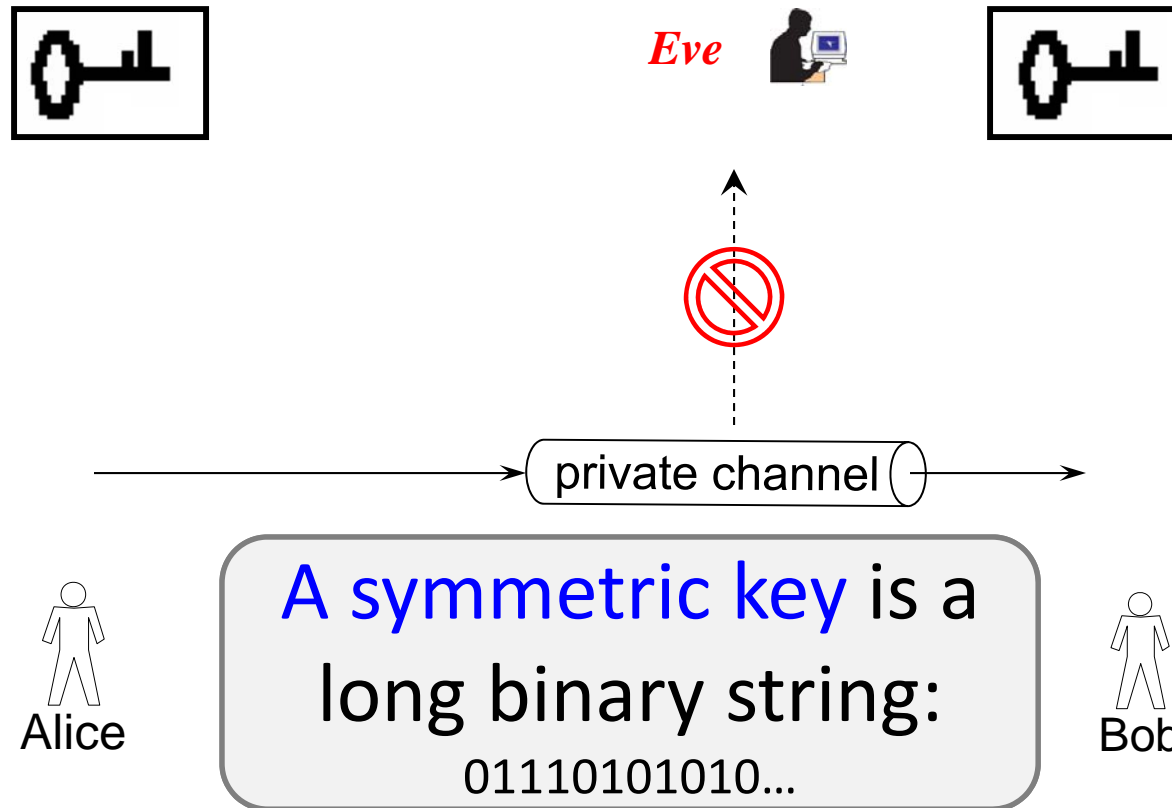
- Assume that password length = 8, **how many** passwords can we have?
 - The possible alphanumeric set size is $(26 + 26 + 10 = 62)$, thus the possible combination size is $62^8 = 218340105584896$ (**$\approx 2^{48}$**)
 - $\{\text{'!@#$%^&*()~';;./:~<>?|{}[]\}\} = 90$, thus the total combinations are at most 127^8
 $\approx 2^{56}$

Roughly 4 seconds for the fastest computer

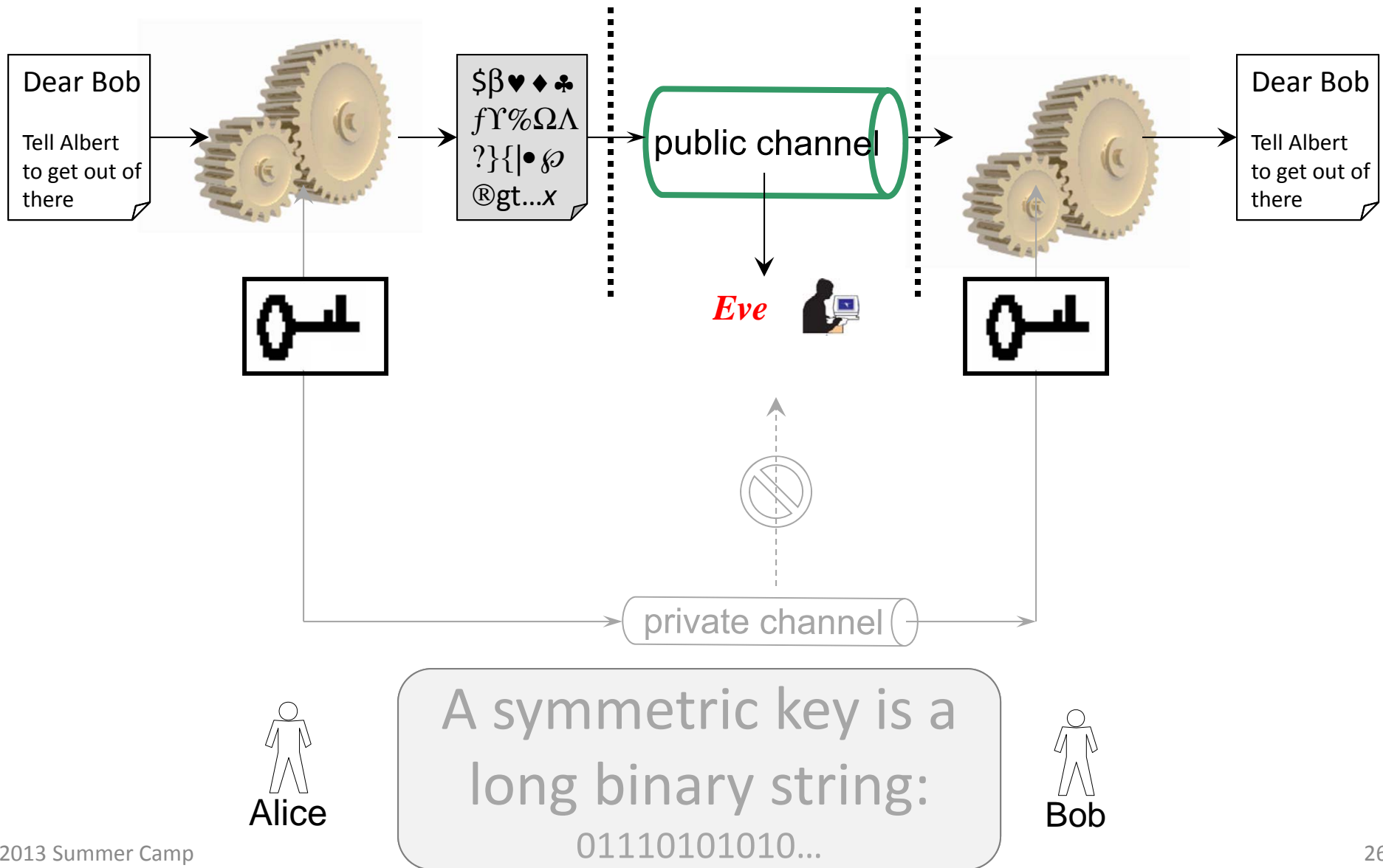
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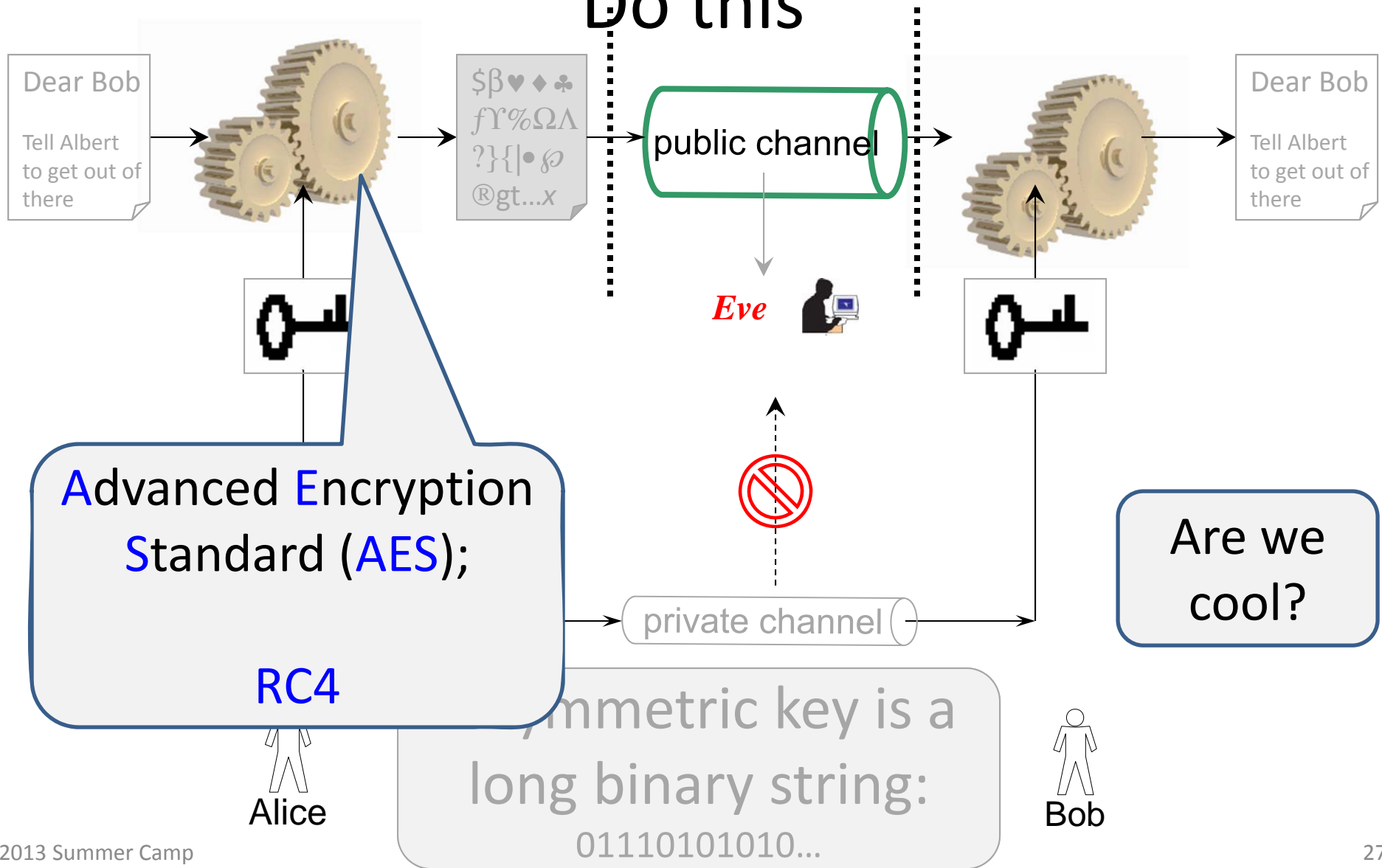
Symmetric Key Encryption



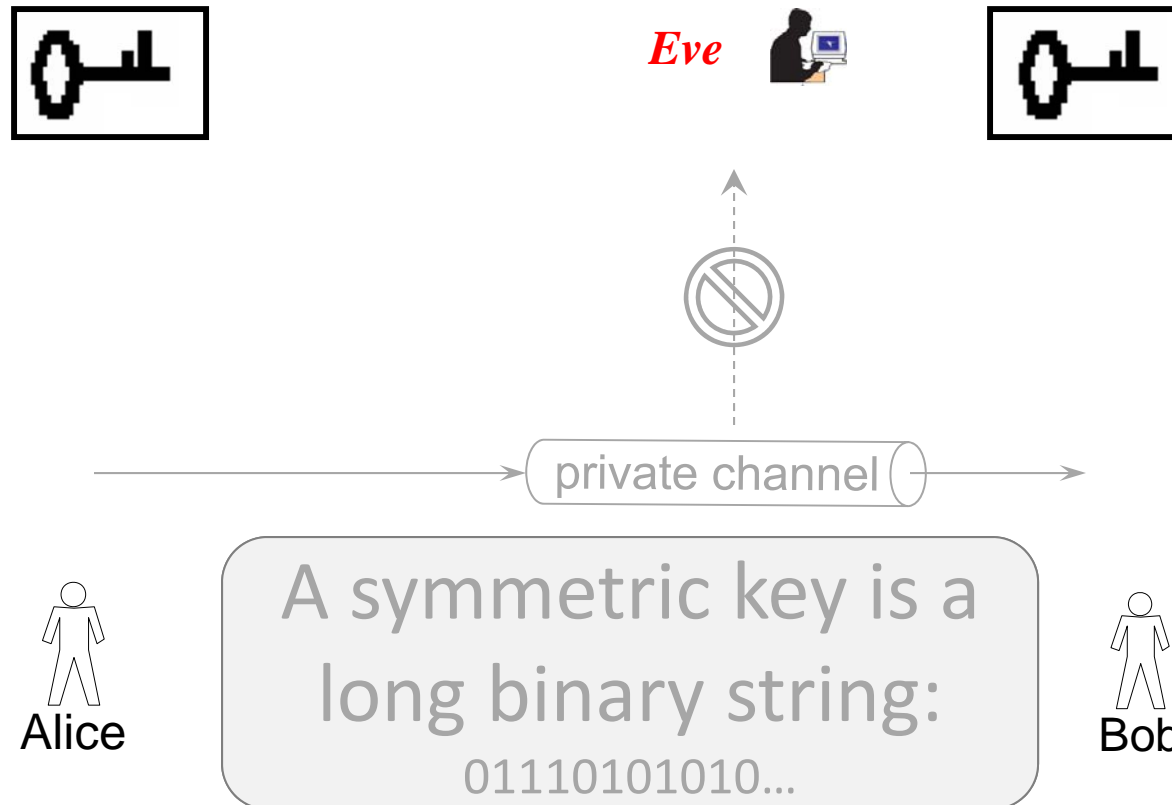
Symmetric Key Encryption



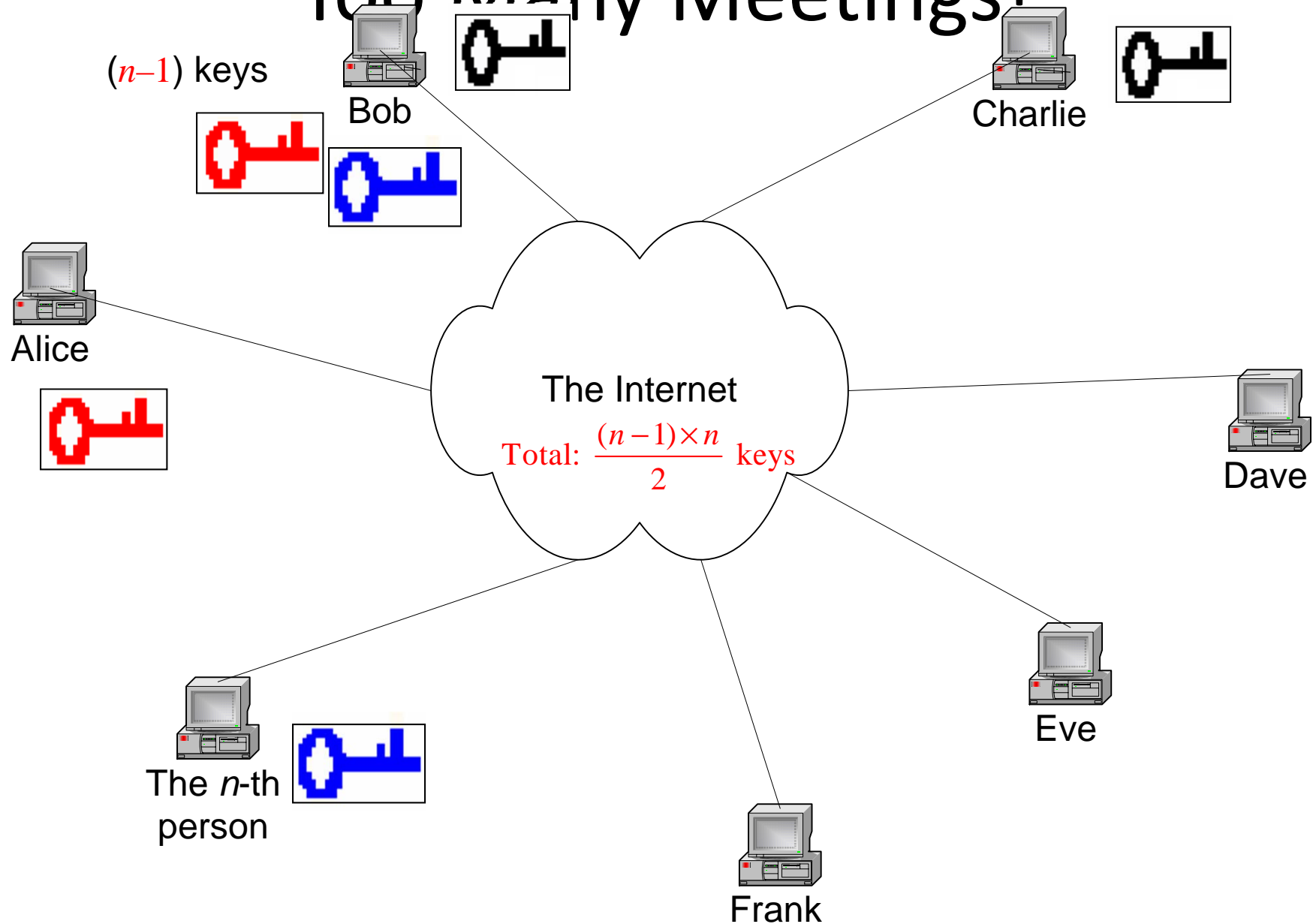
After 2000 years, We Know How to Do this



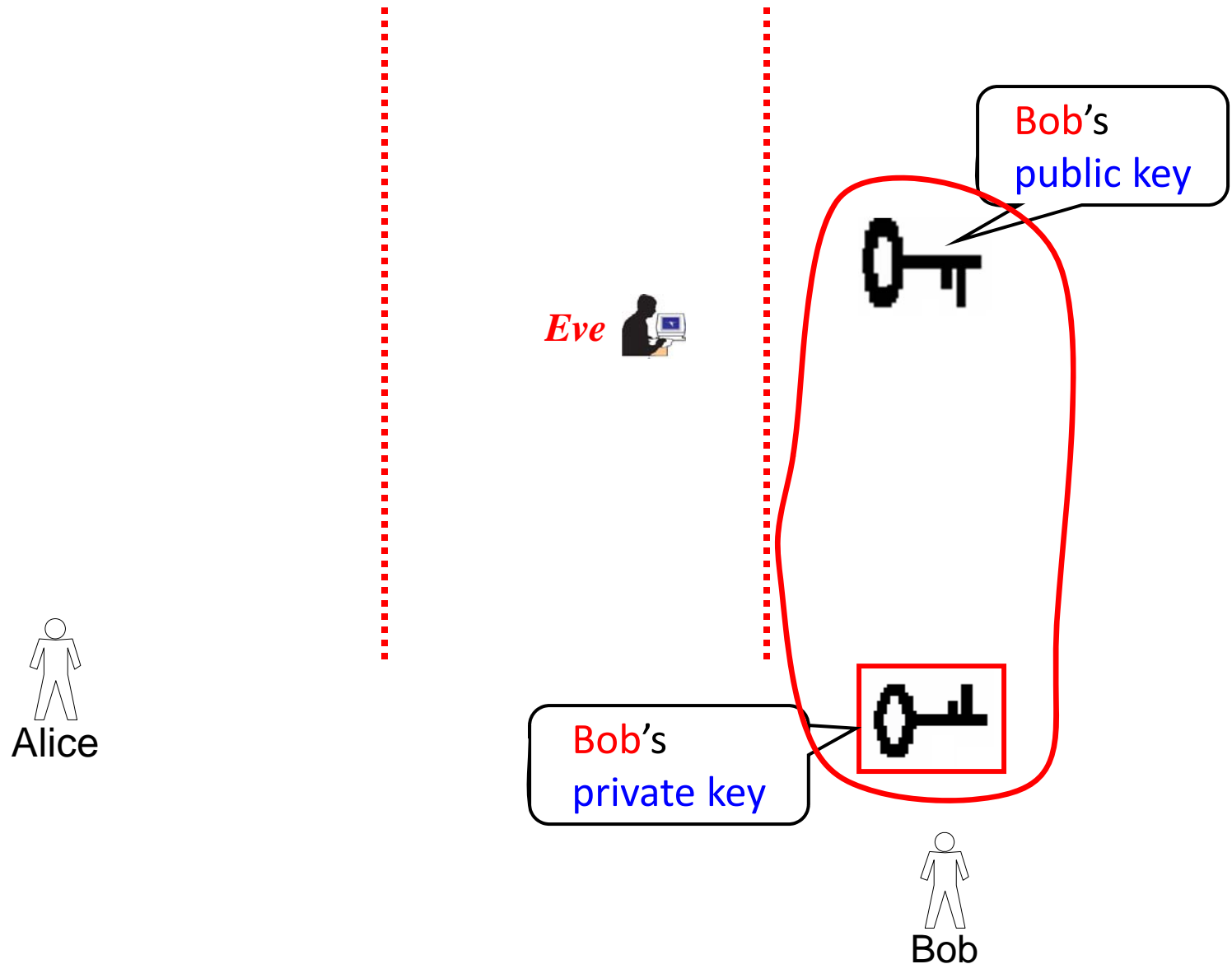
Personal Meetings?



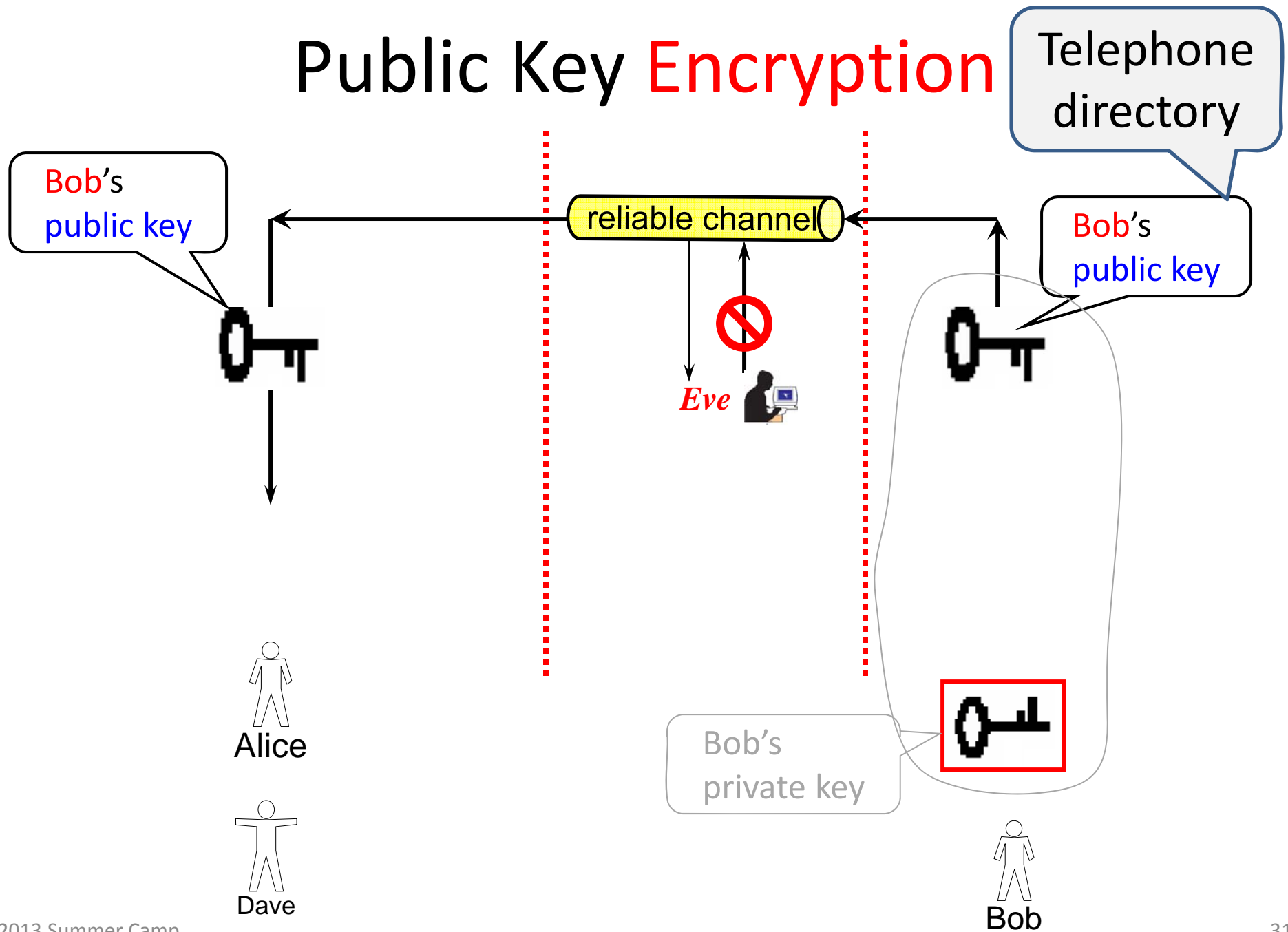
Too Many Meetings!



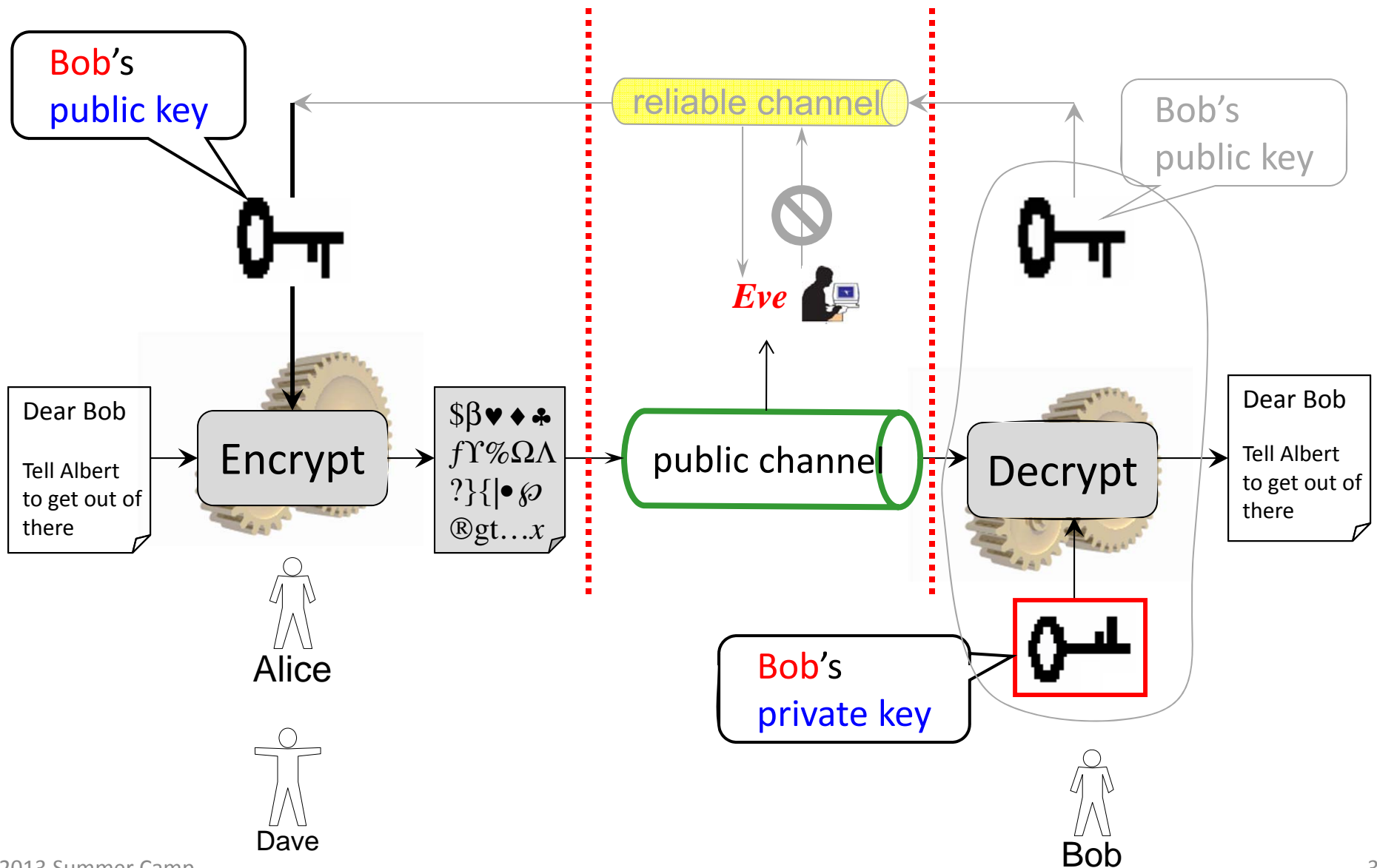
Public Key Encryption (after 1970s)



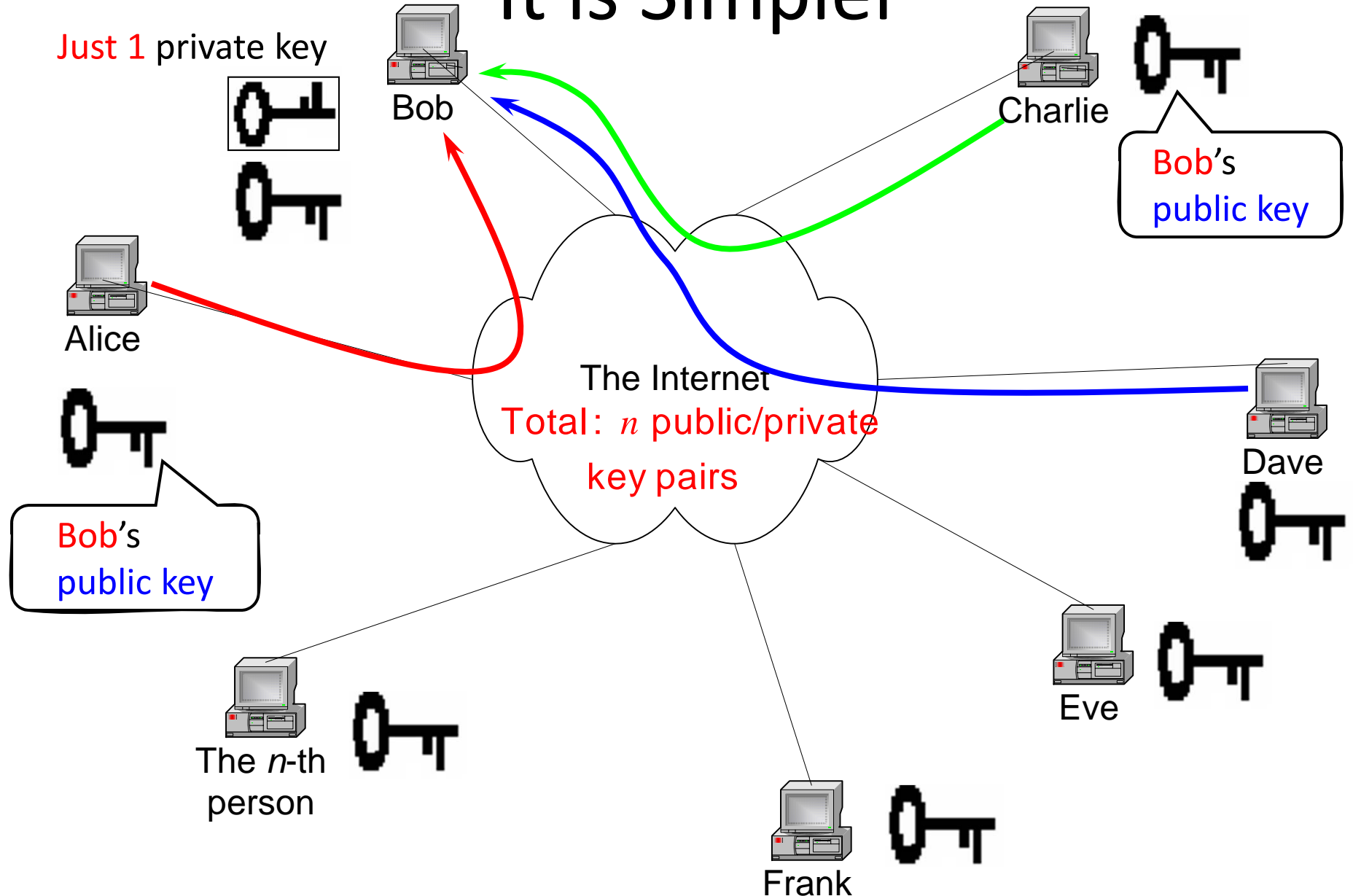
Public Key Encryption



Public Key Encryption



It is Simpler



Algorithm Buzzwords

- Symmetric key encryption algorithms
 - Advanced Encryption Standard (AES)
 - RC4 (Ron's Cipher 4)
- Public-key encryption algorithms
 - RSA: Rivest-Shamir-Adleman
 - Elliptic-curve encryption

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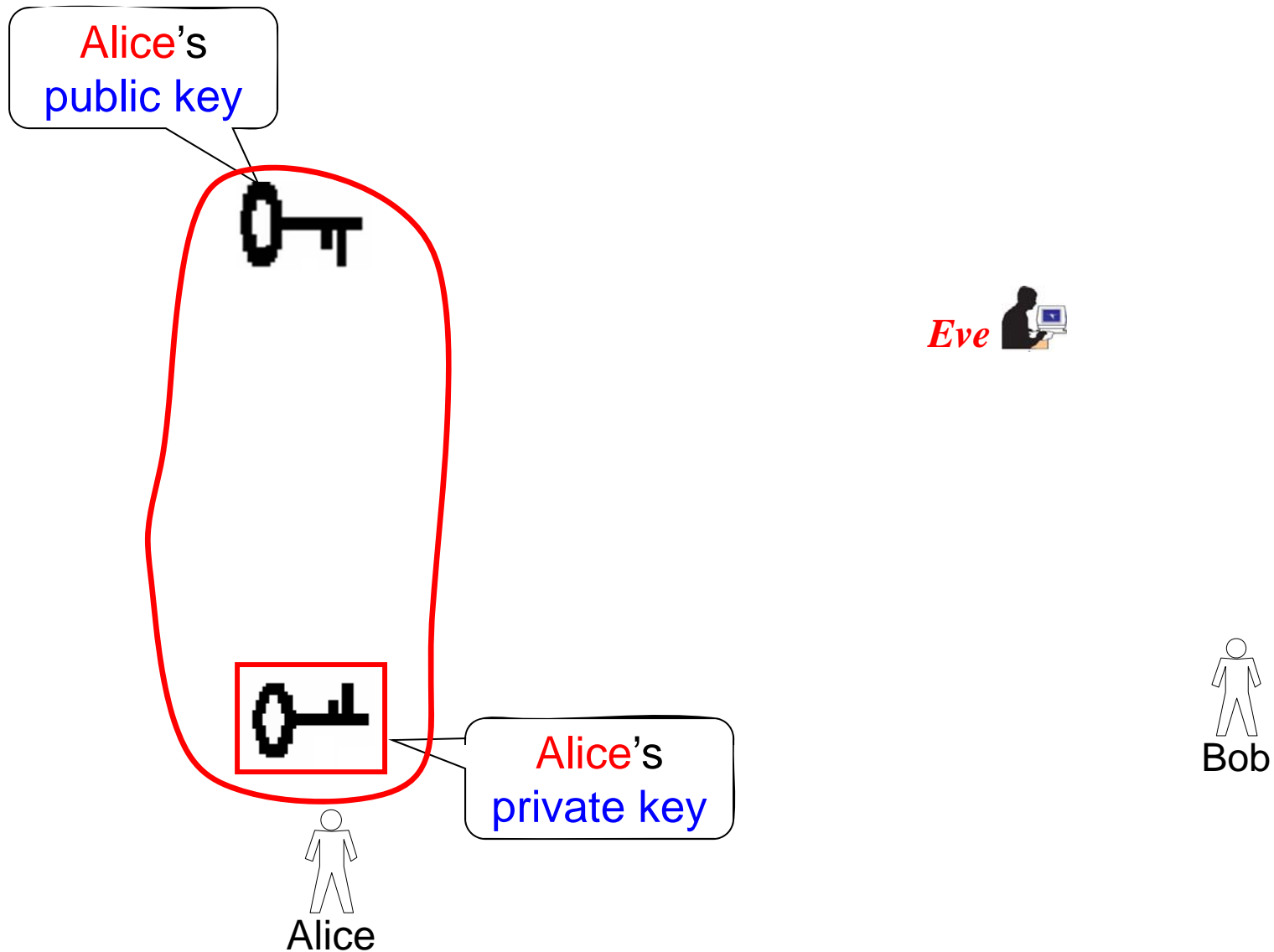
Signatures?

- Eat in a restaurant?
 - Sign your credit card payment
- Rent a house?
 - Sign the contract
- Get a car loan?
 - Sign the contract

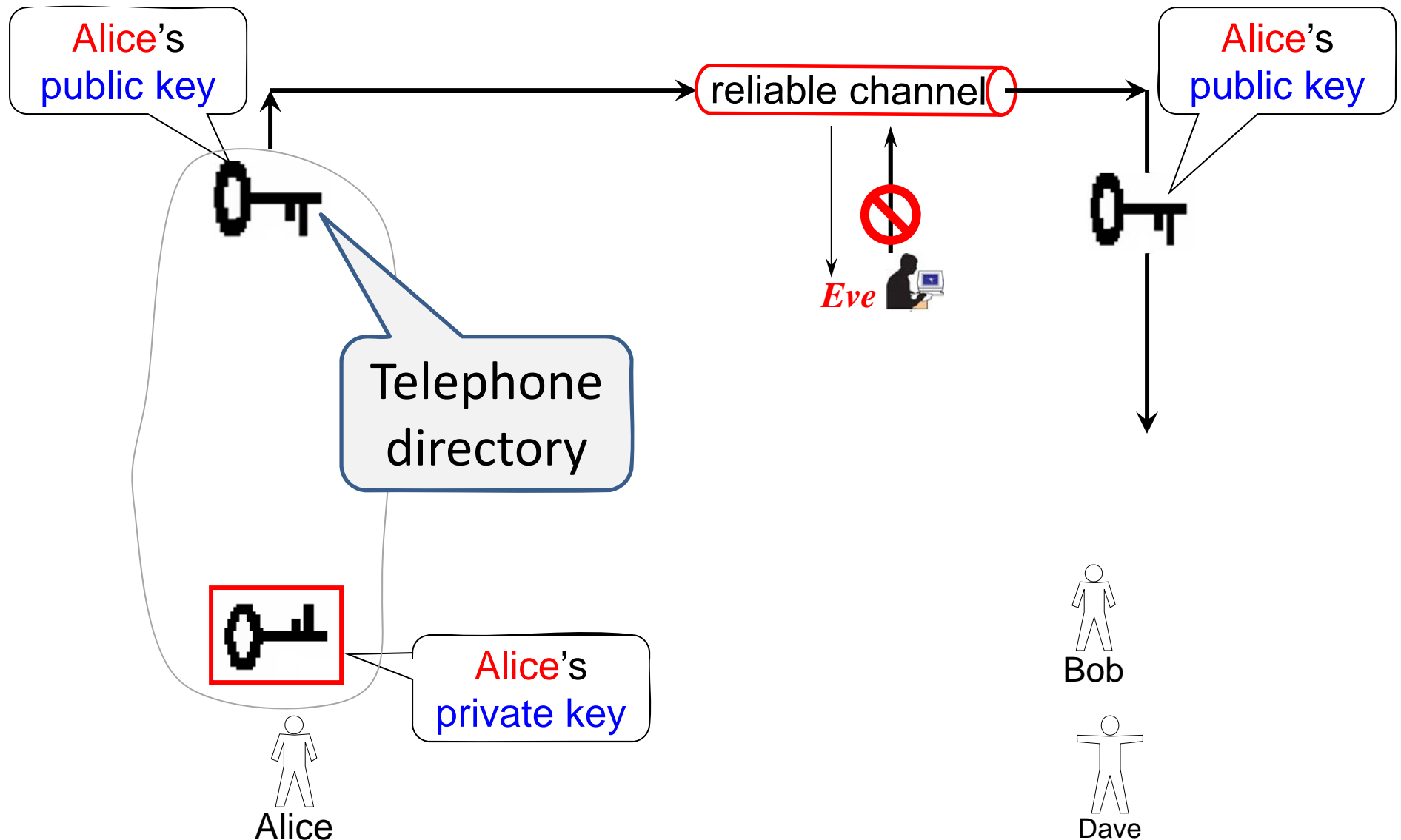
Can we implement the concept of signature in the **digital** world?

Handwritten signatures can be copied: does **not** work well in the **digital** world

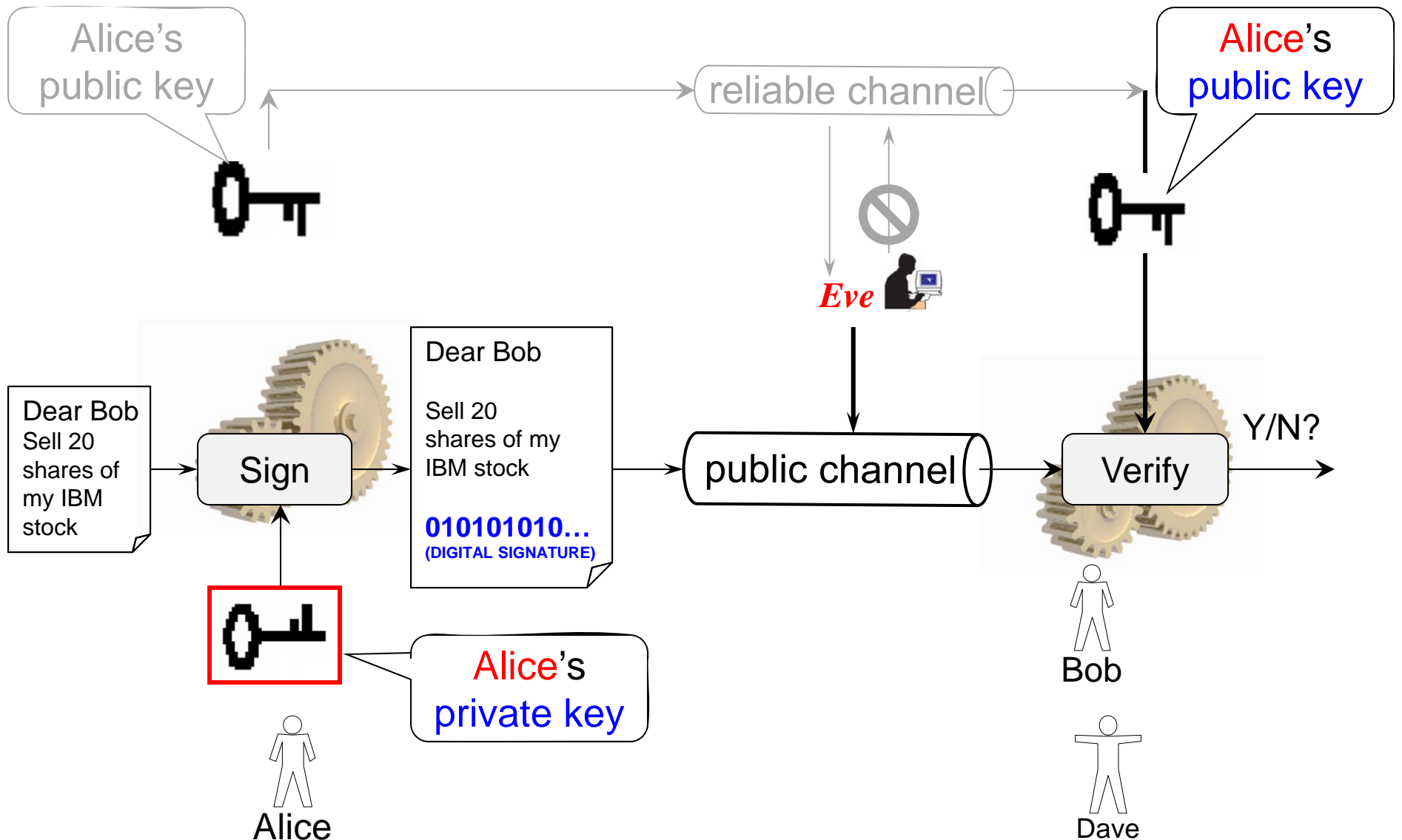
Public Key Digital Signature



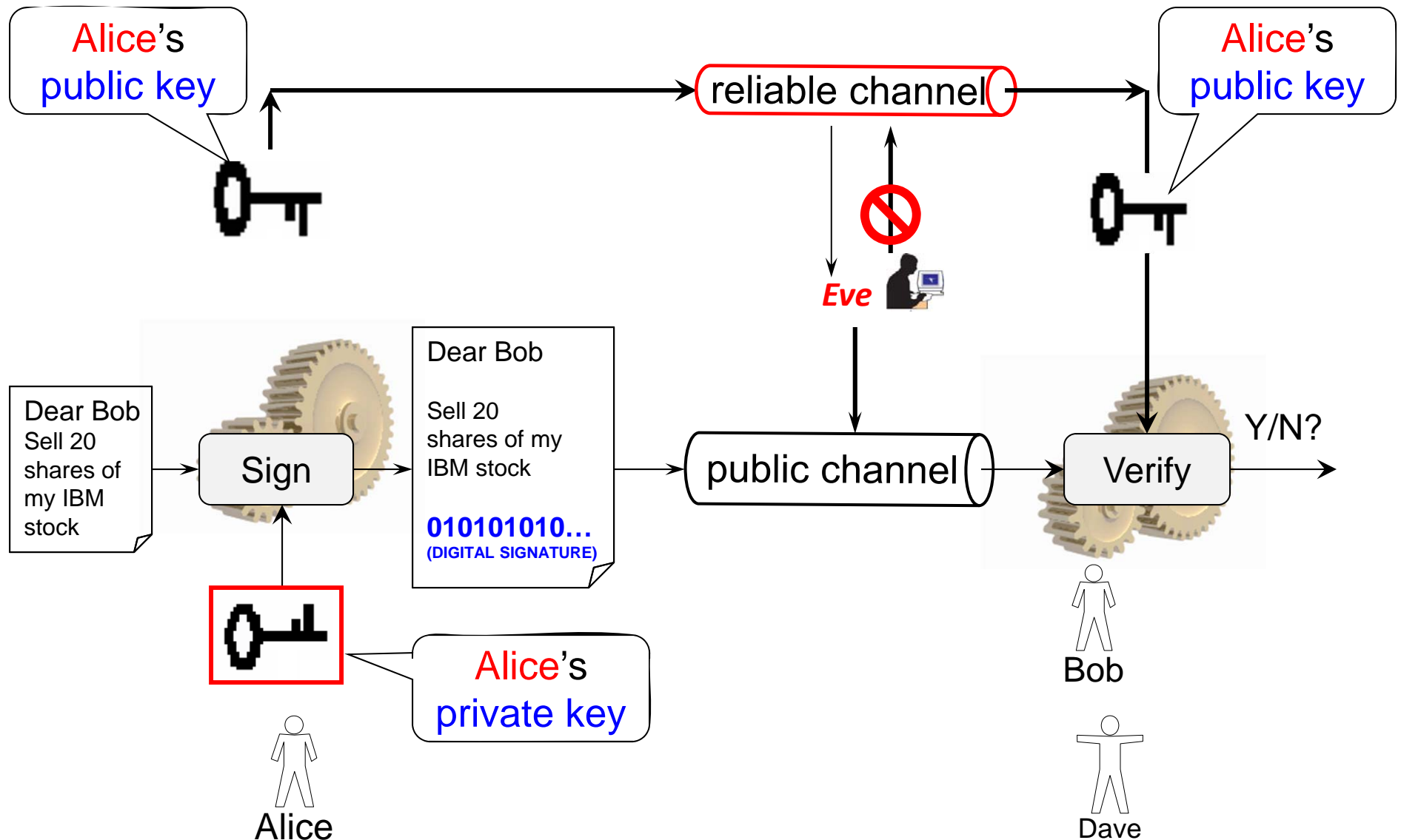
Public Key Digital Signature



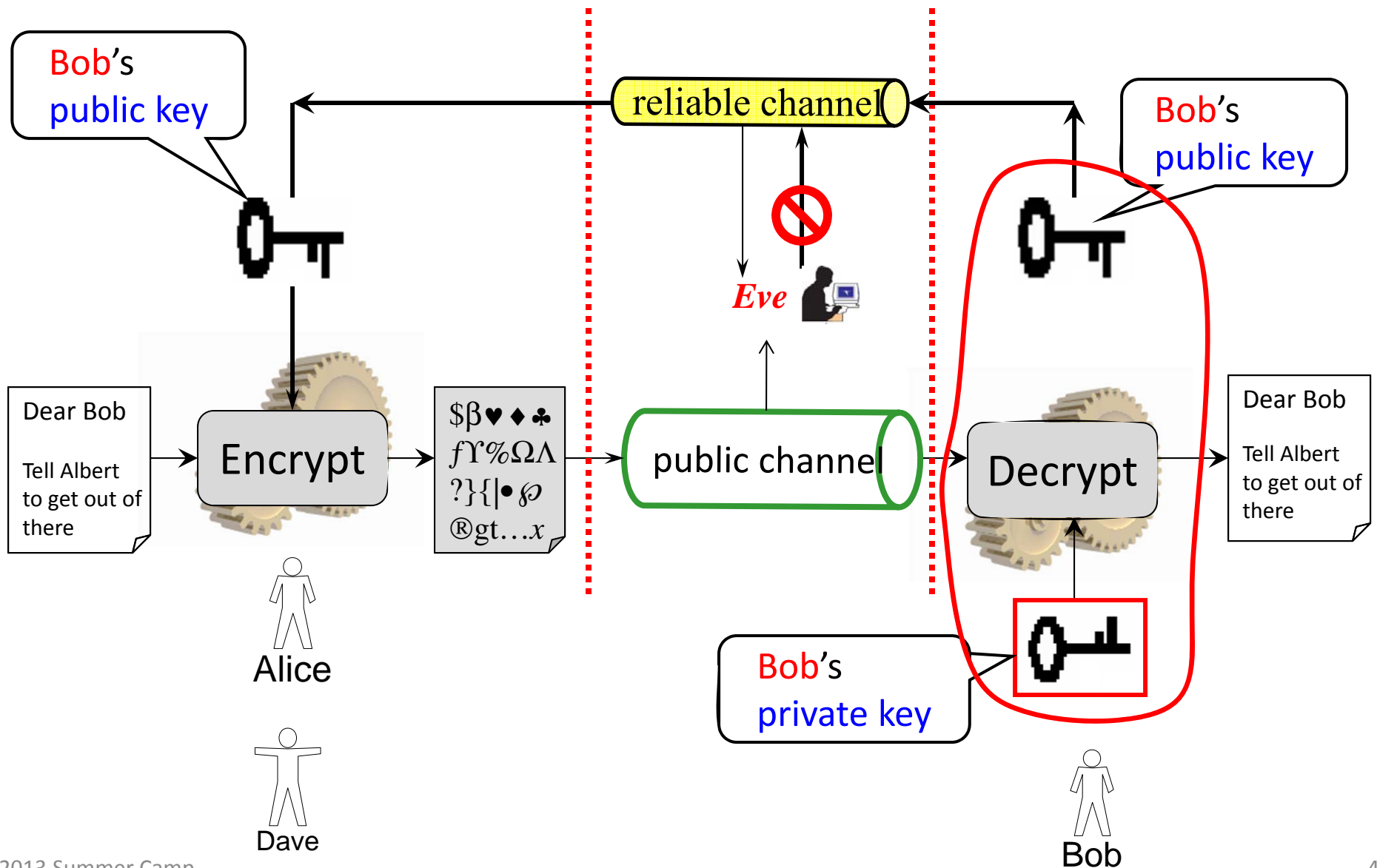
Public Key Digital Signature



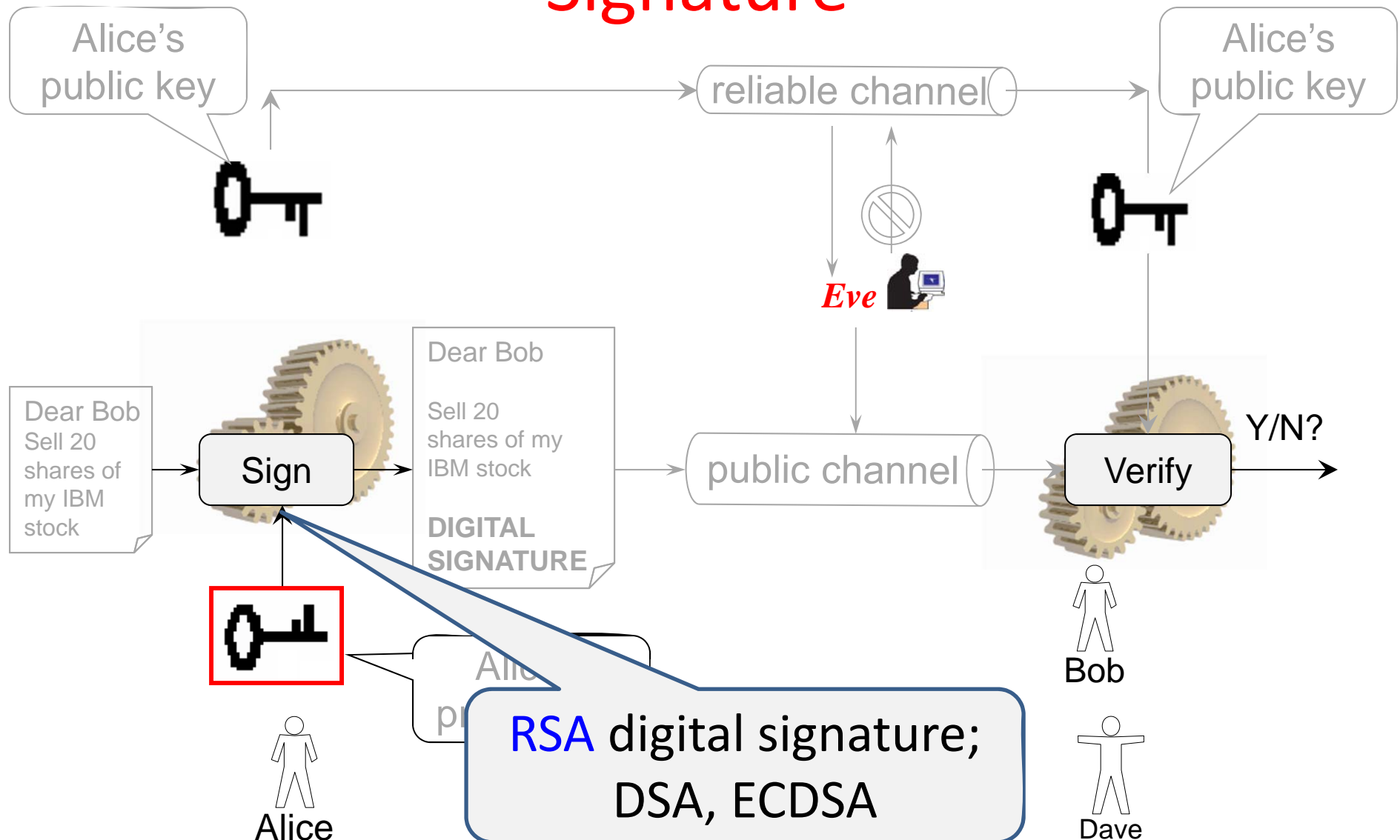
Public Key Digital Signature



Public Key Encryption



We Know How to Implement Digital Signature



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One-way?

- One-way roads
 - You are **not supposed** to go the other way
 - But you can (break the law)

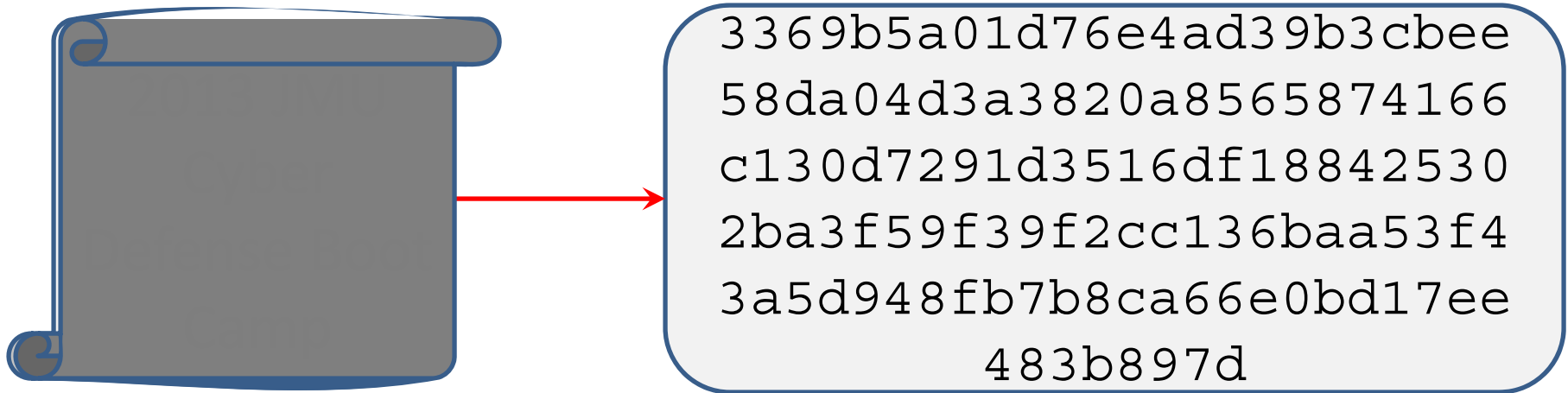


One-way Cryptographic Function?

- A big file: 4G bytes, called m
- For any function h , $y \leftarrow h(m)$
- **IF** for some special function h , given any value y , it is hard (for you/anybody) to find x such that $y = h(x)$
 - h is called **one-way function**
 - You can try, but you won't be able to computationally (**un**like one-way roads)
- Most functions are **not** one-way
- One-way functions are useful for information security

Example

- SHA512 is a cryptographic hash function

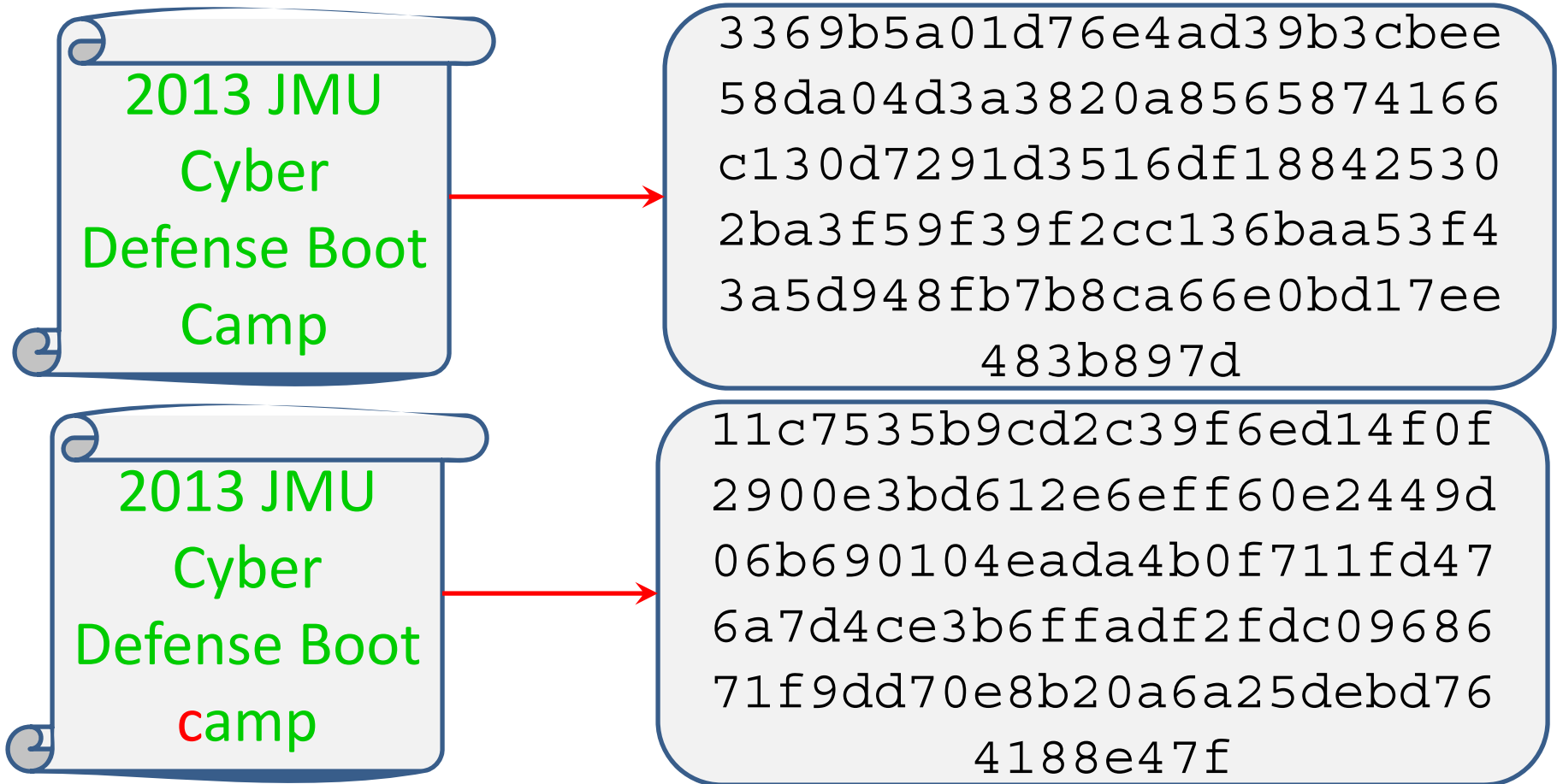


Cryptographic Hash Function

- For function h , $y \leftarrow h(m)$
- If m is always much larger than y , h is a compression function
- Form some special compression function h , it is hard to find **any pair** (x, y) , $x \neq y$, such that $h(x) = h(y)$, h is called **collision resistant**
 - **Not** collision proof
- If h is both one-way **and** collision resistant, h is called a **cryptography hash function**

Example

- SHA512 is a cryptographic hash function

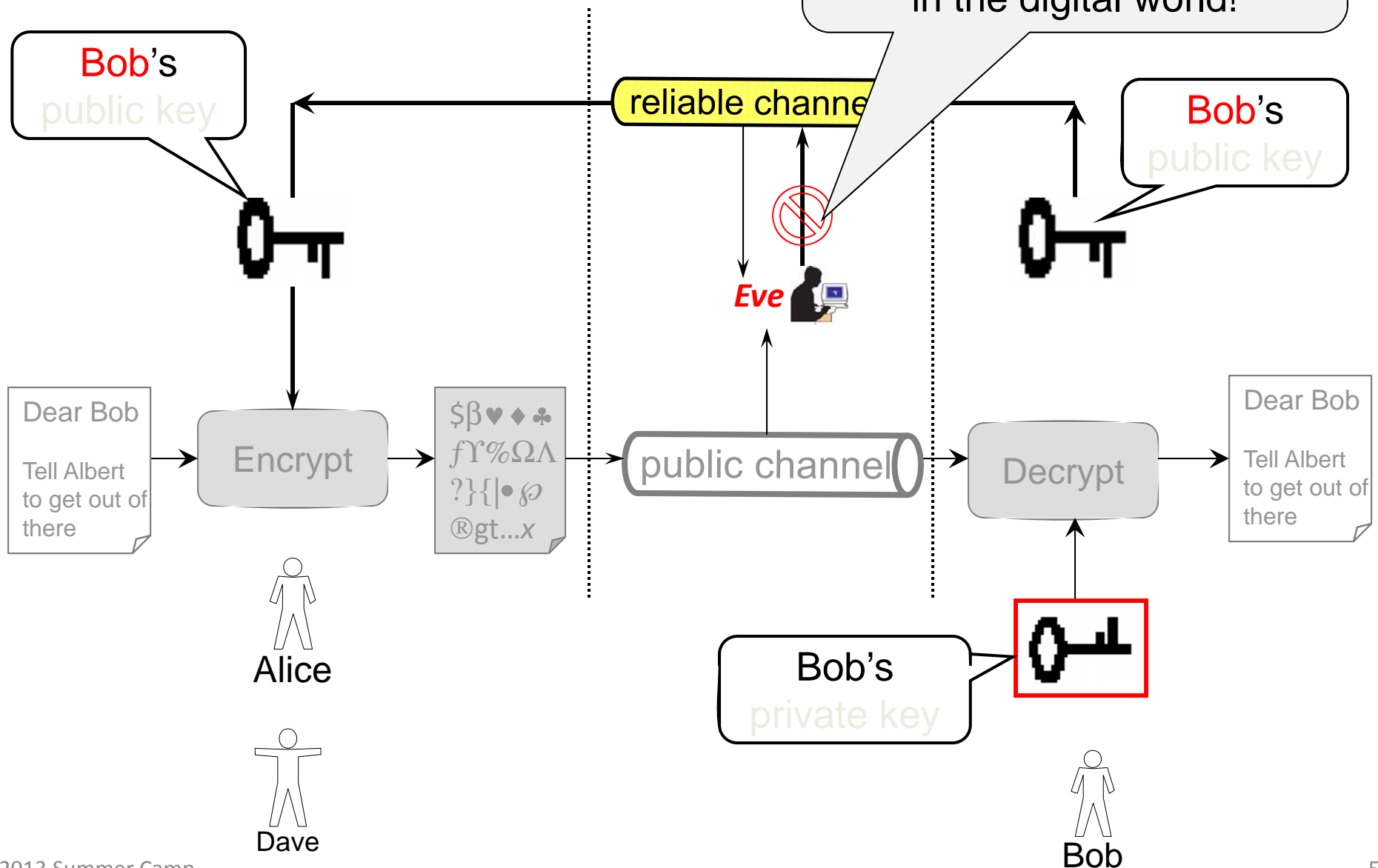


Road Map

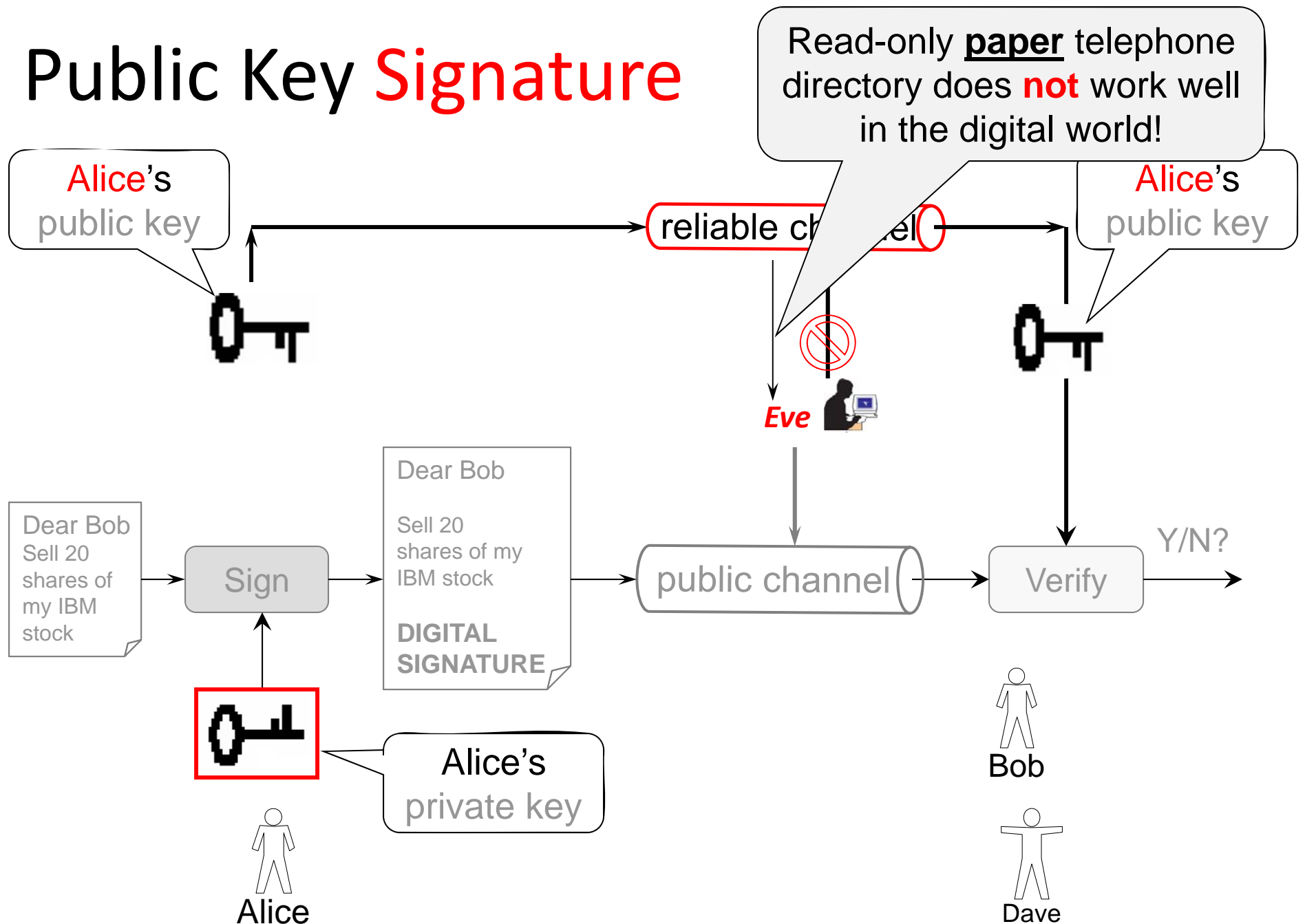
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Public Key Encryption

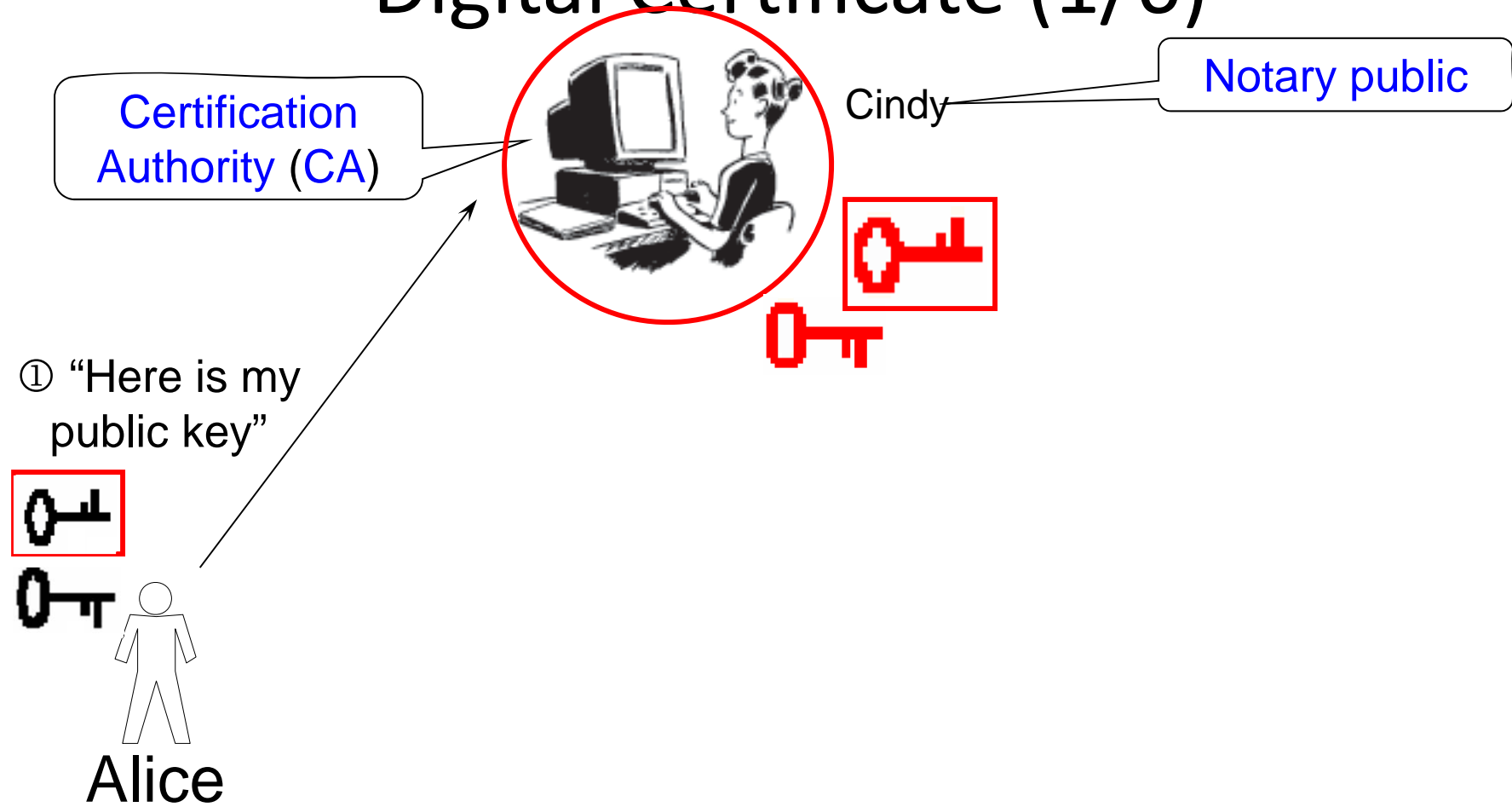
Read-only paper telephone directory does **not** work well in the digital world!



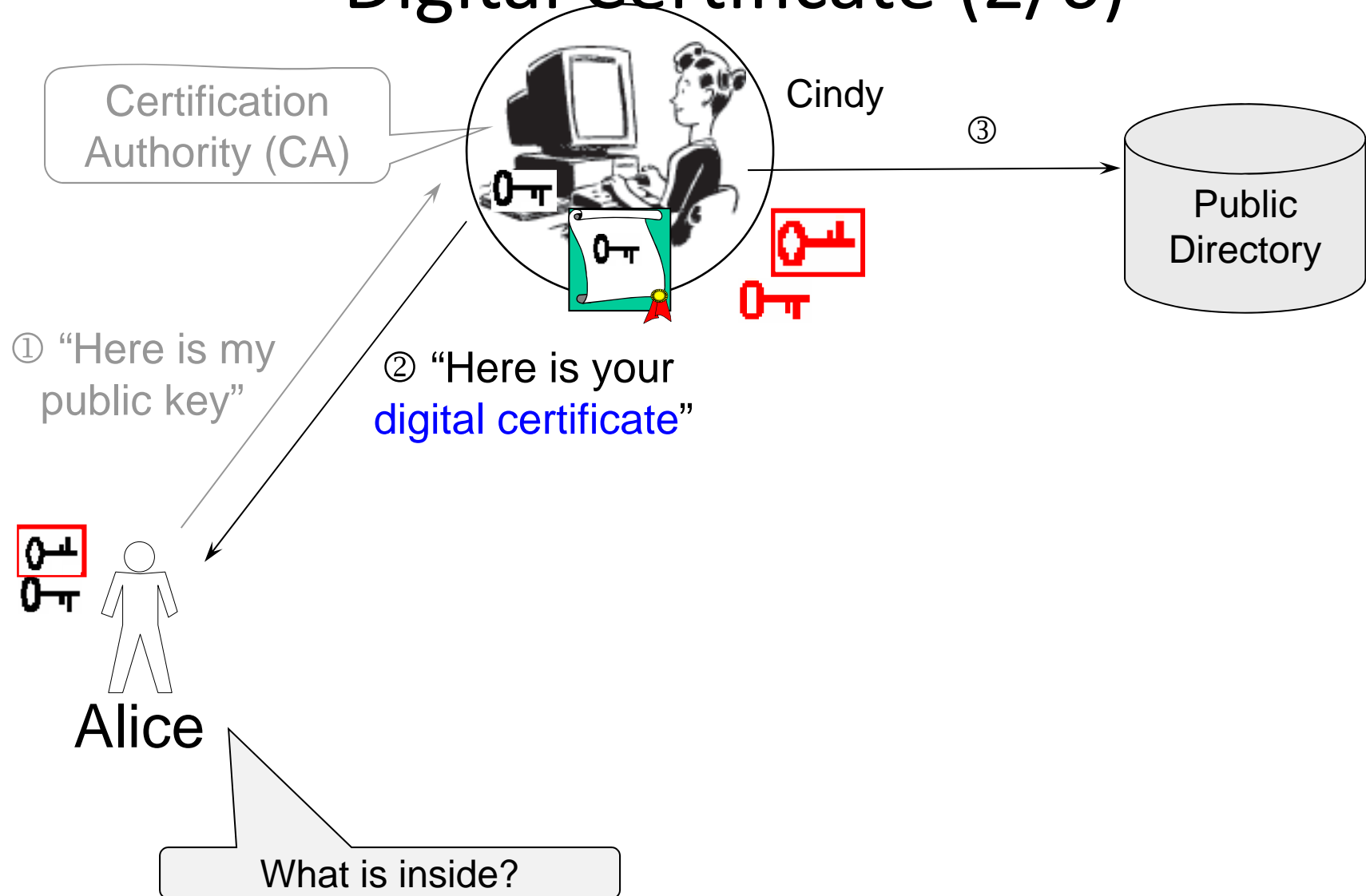
Public Key Signature



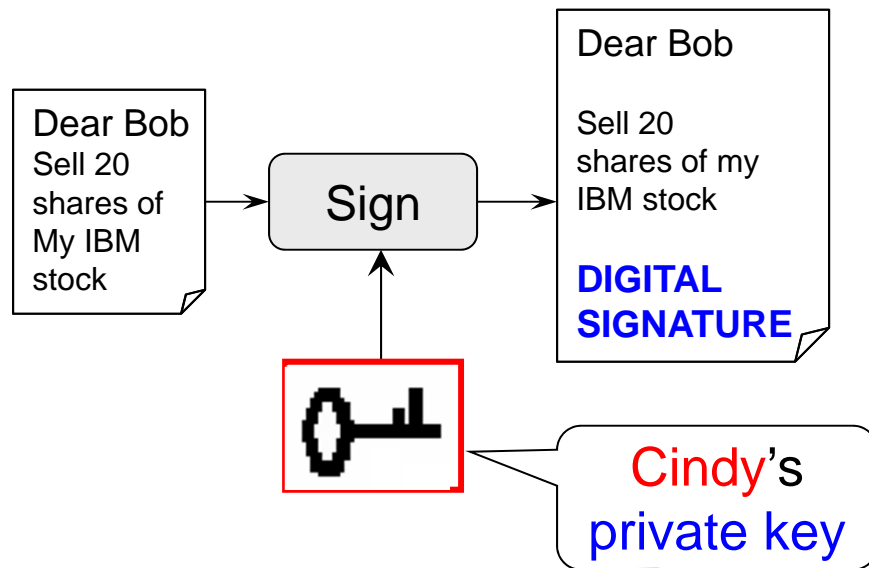
Digital Certificate (1/6)



Digital Certificate (2/6)

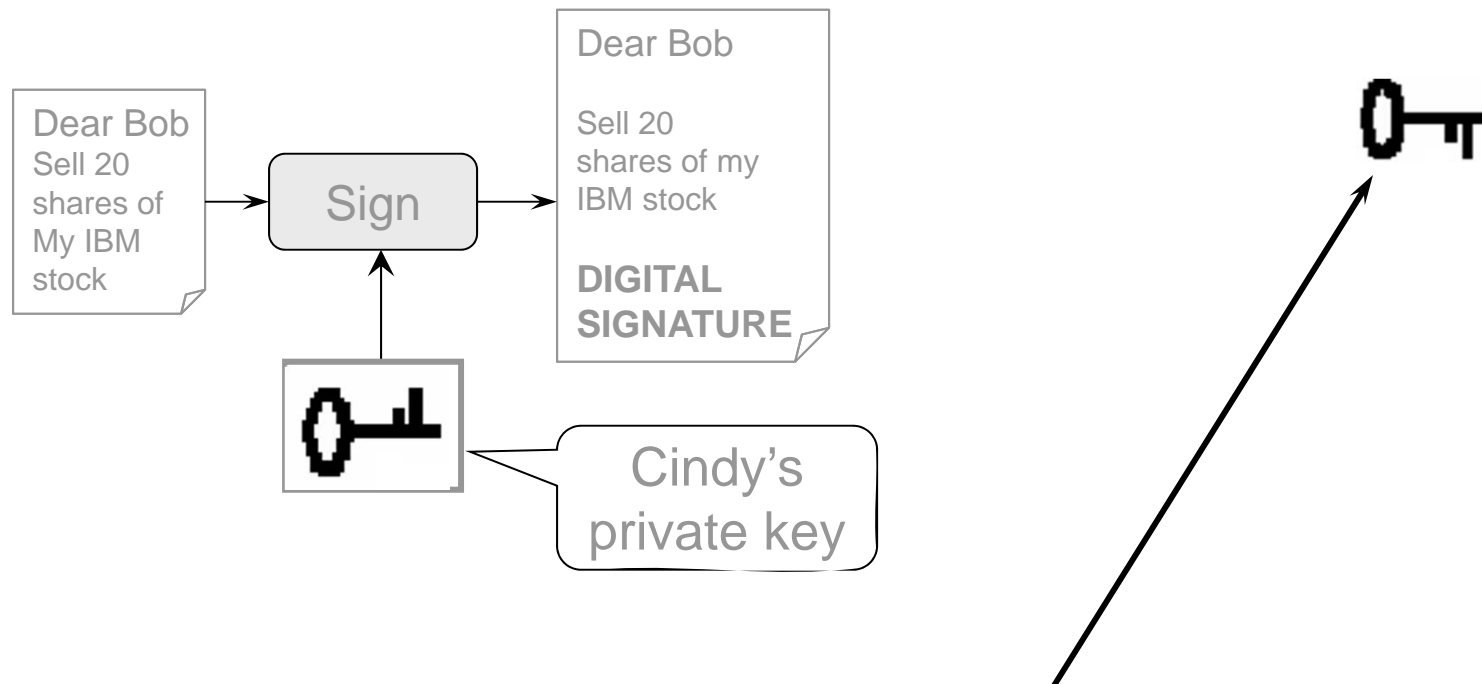


Digital Certificate (3/6)



- Questions:
 - How to verify the authenticity of the signed **message**?
 - What do you need to verify?

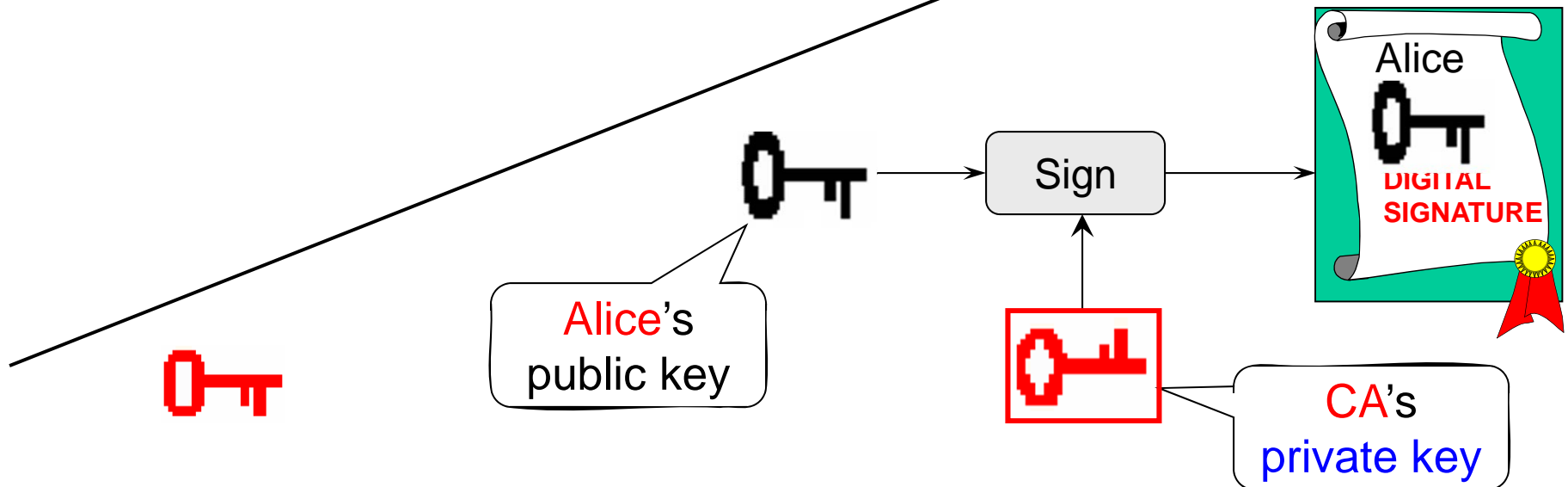
Digital Certificate (4/6)



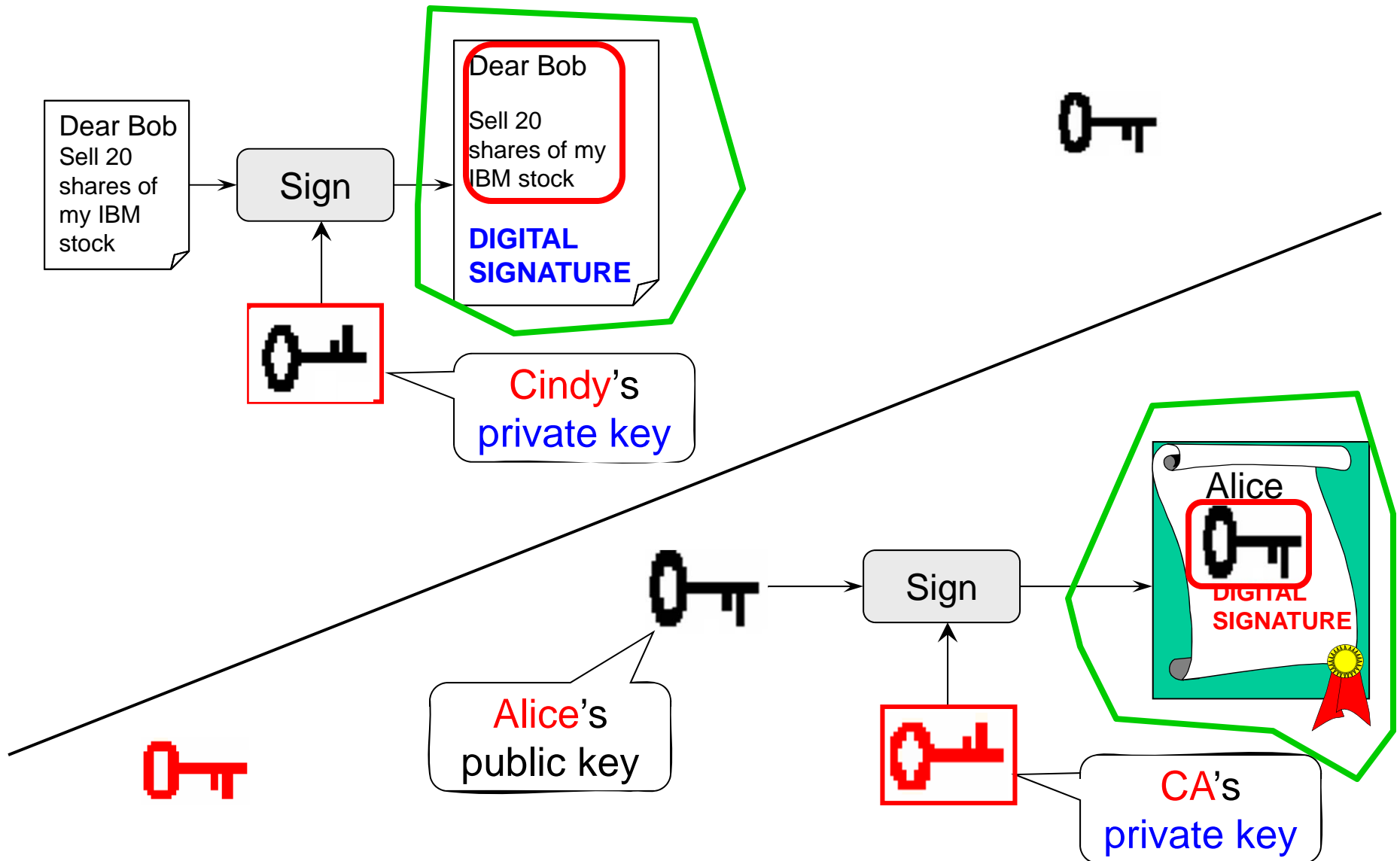
- You need the signer's public key!
- What if you mistook a bad guy's public key as the signer's public key?

Digital Certificate (5/6)

- Why not digitally sign a **public key** before it is distributed?
- How to verify the authenticity of the digitally signed public key?



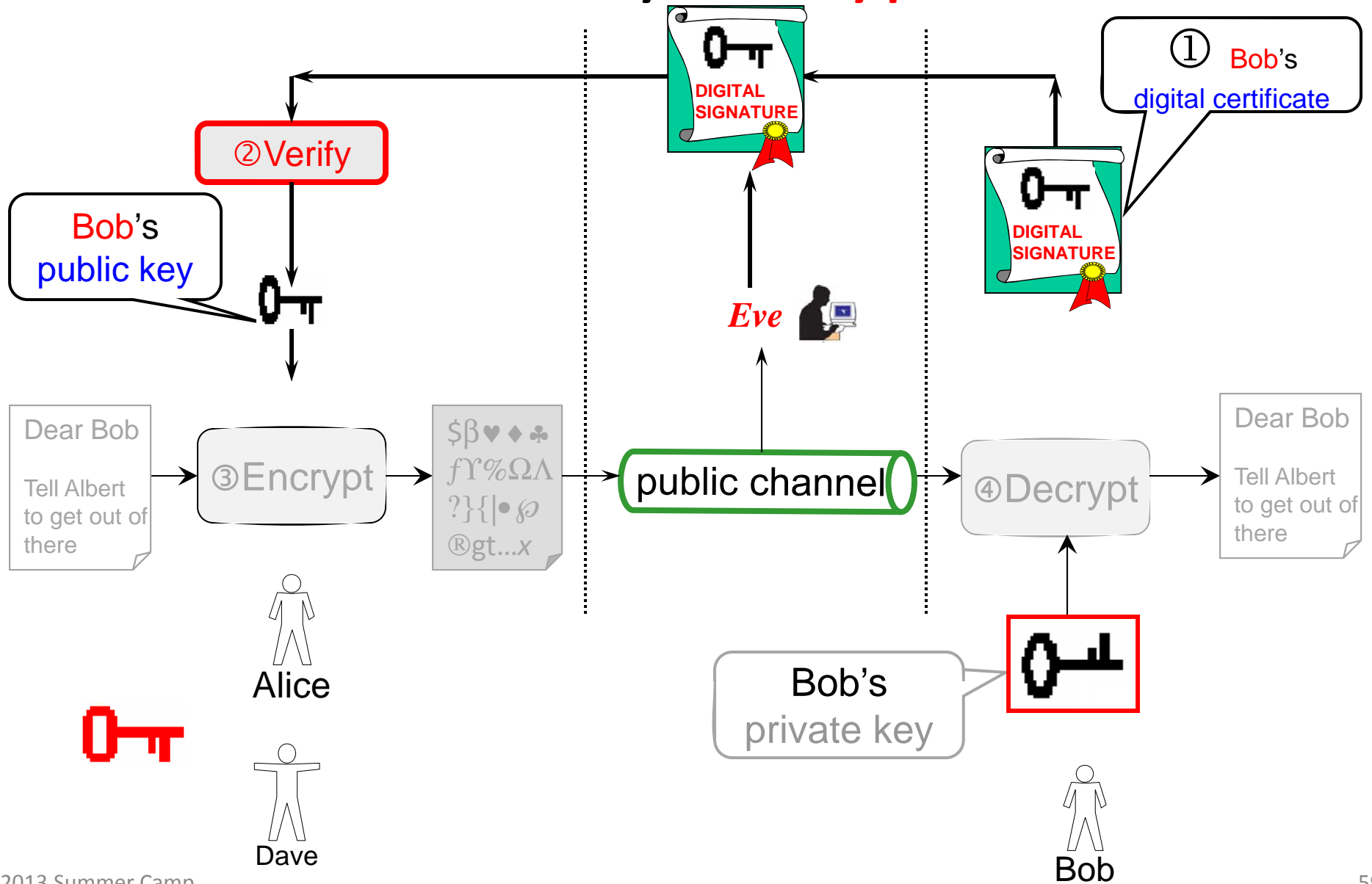
Digital Certificate (6/6)



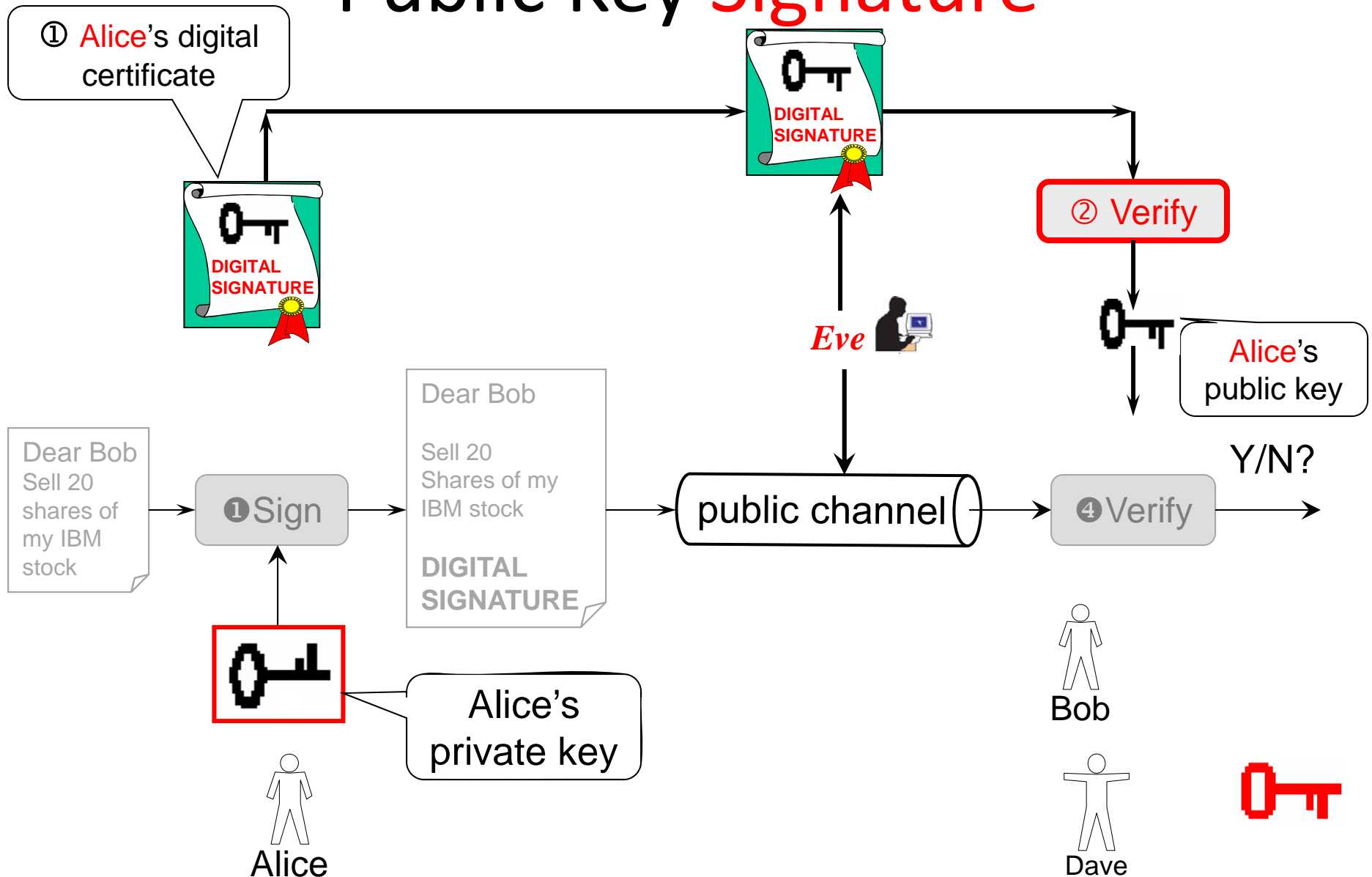
Inside a Digital Certificate



Public Key Encryption



Public Key Signature



Quotes from Don Davis

- **Q:** How is a key-pair like a hand grenade?
- **A:** You get two parts, there's no aiming, & it's hard to use safely



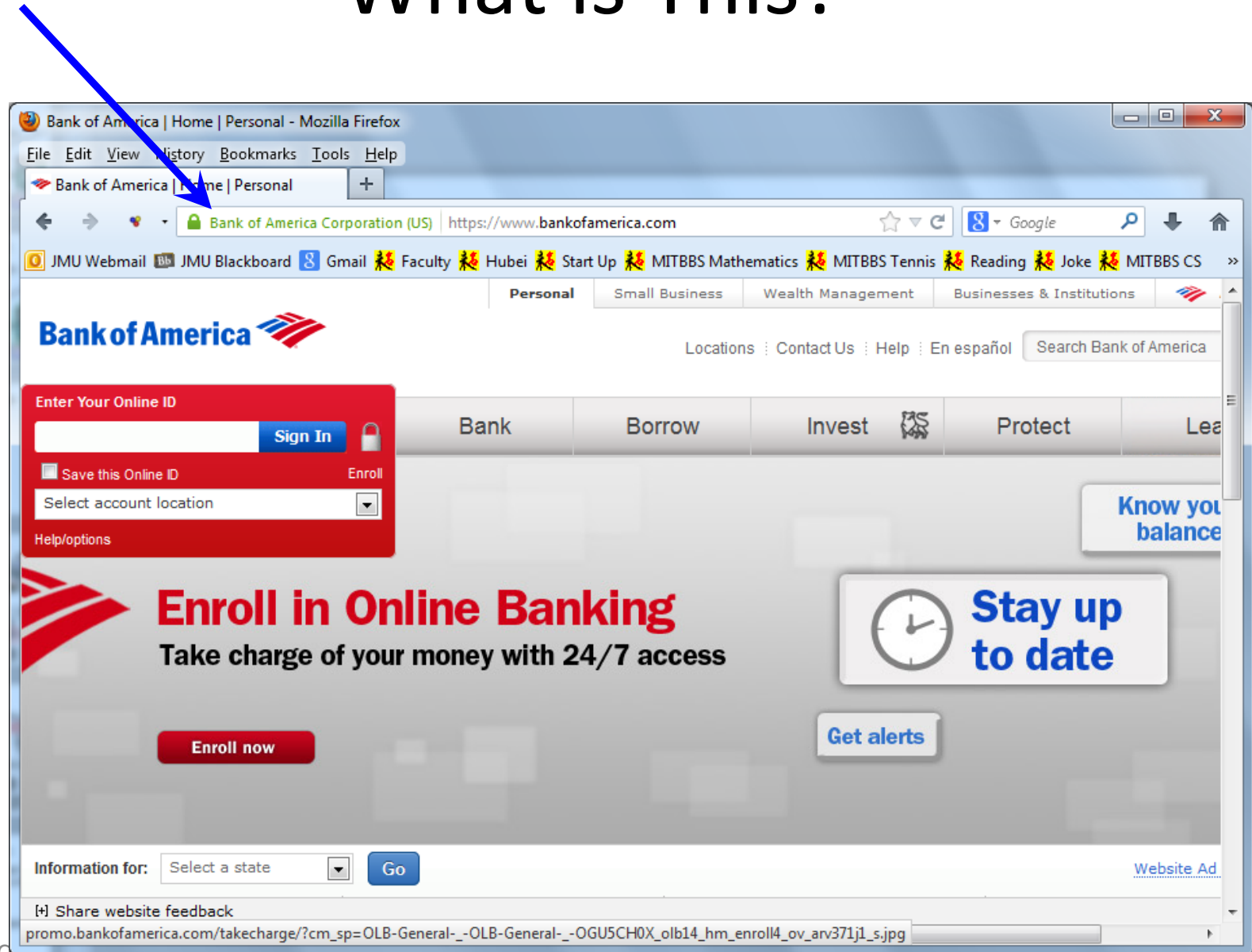
- **Q:** How are they different?
- **A:** With a grenade, you throw the dangerous part away ...

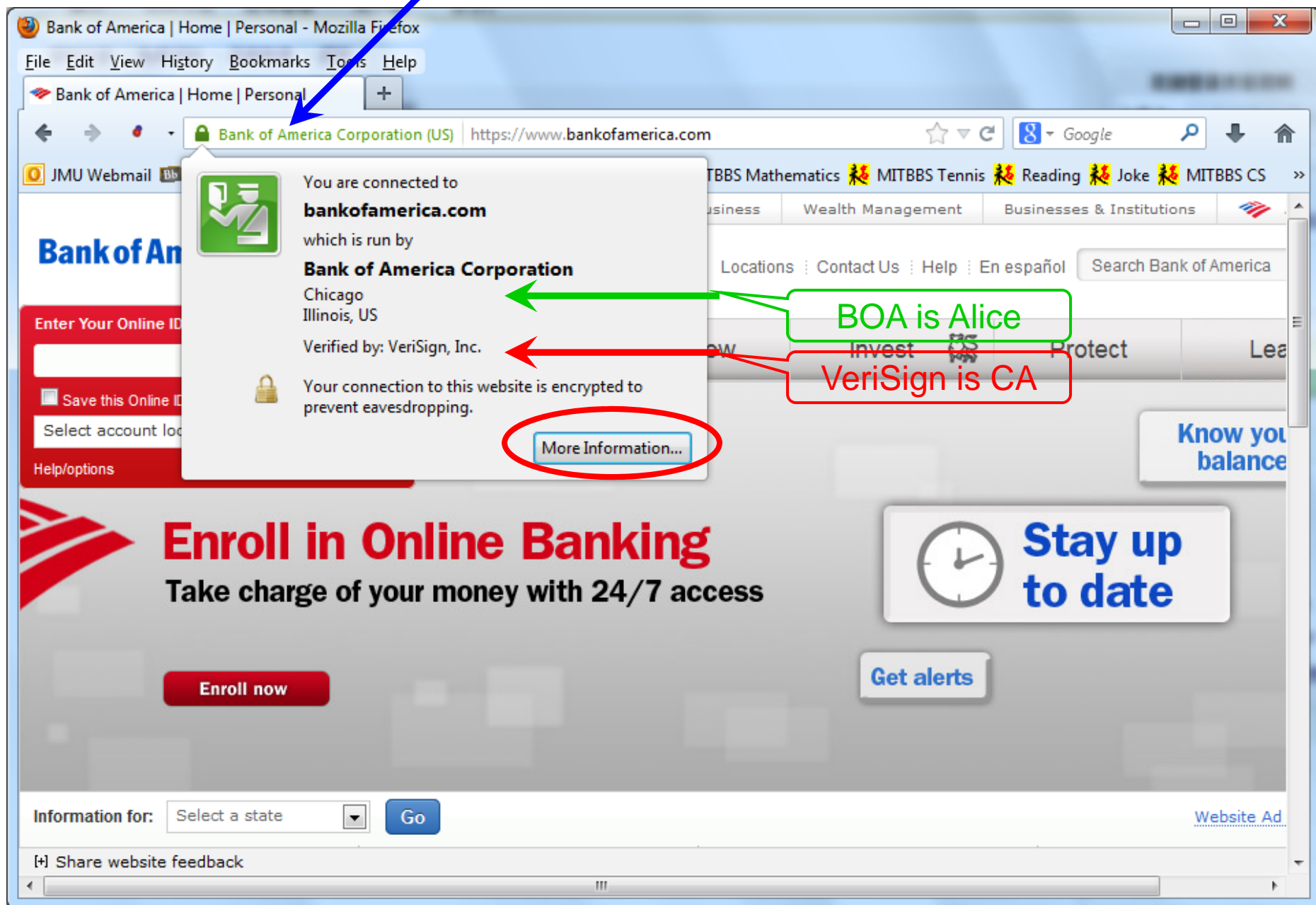


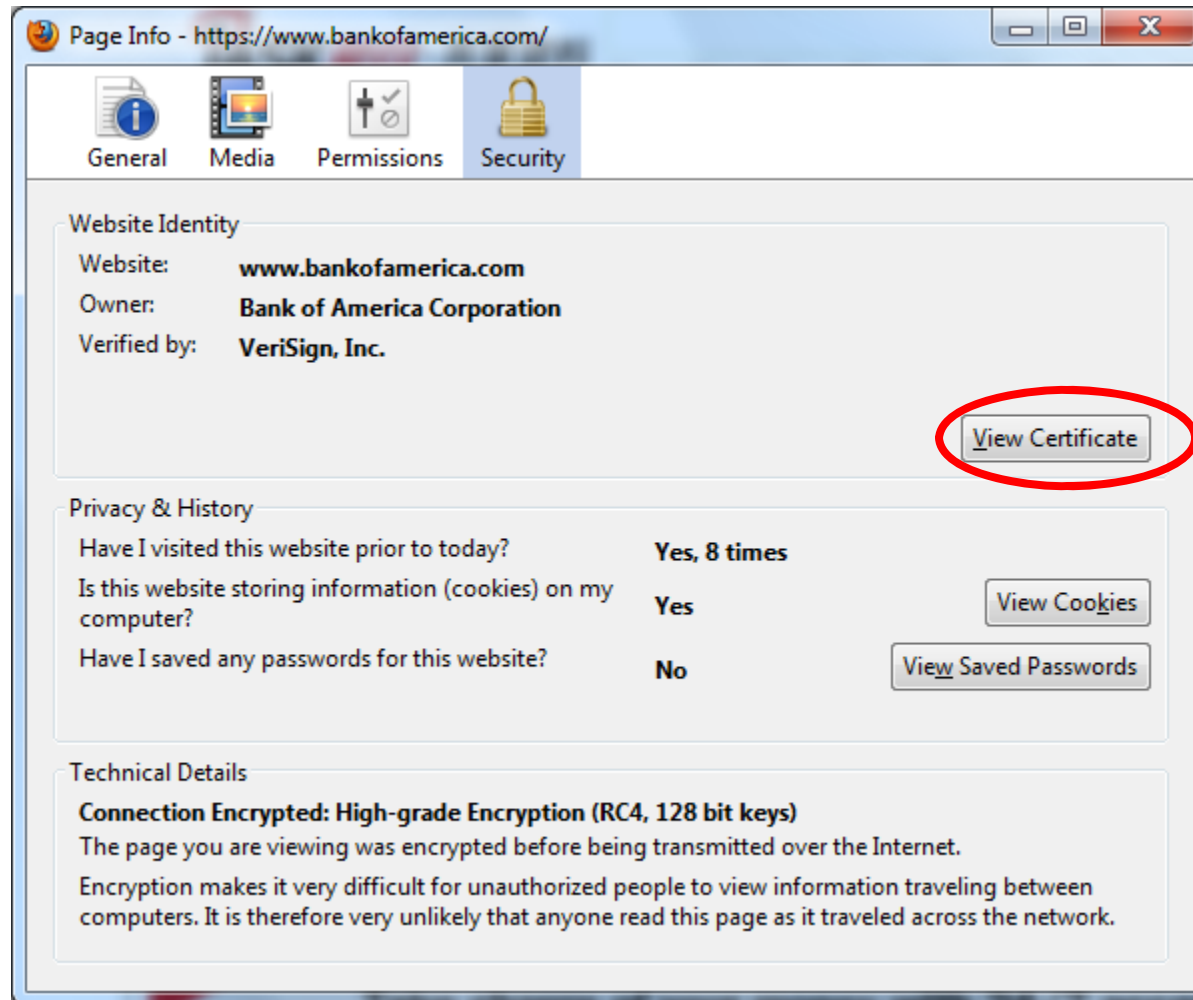
Road Map

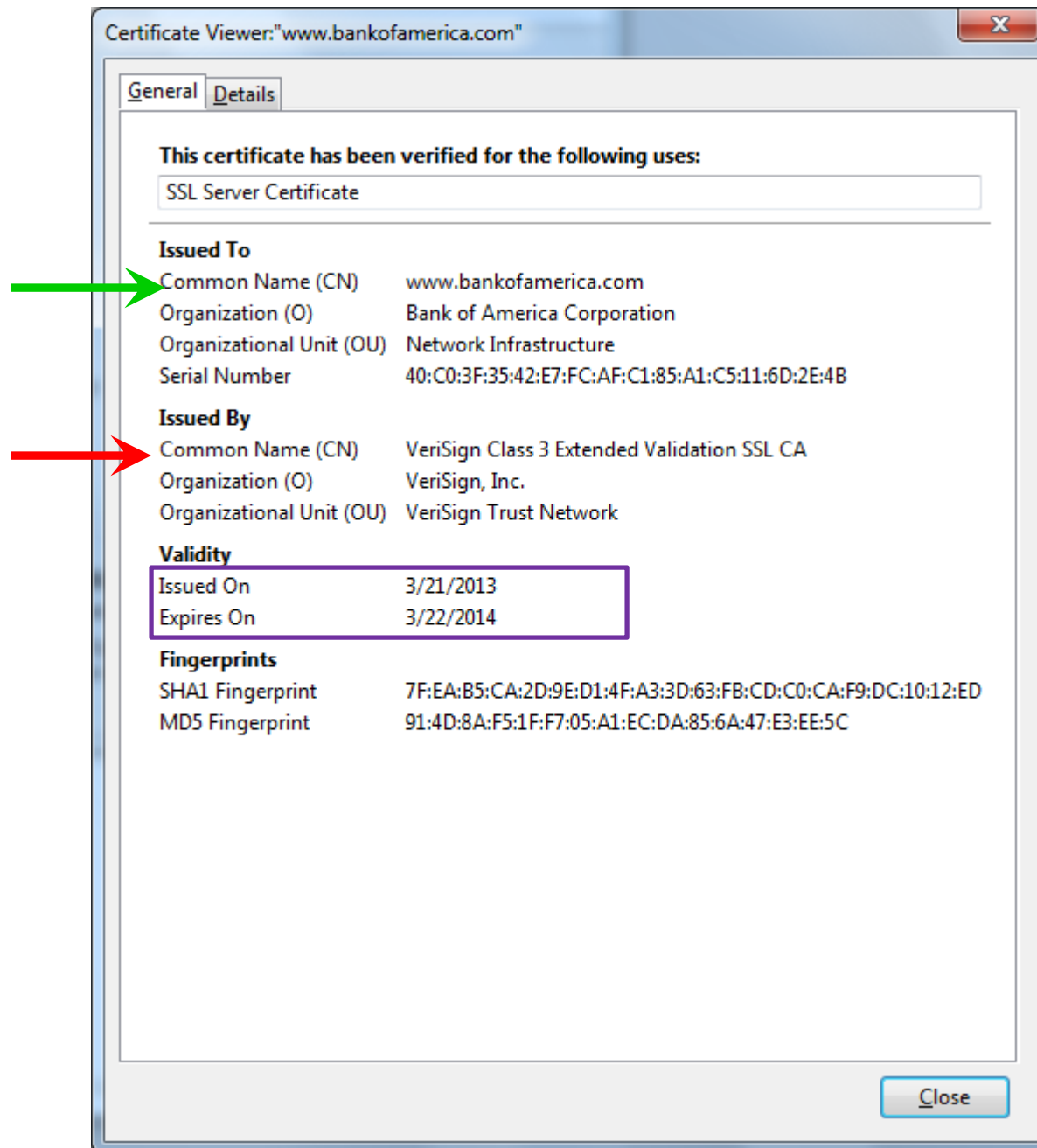
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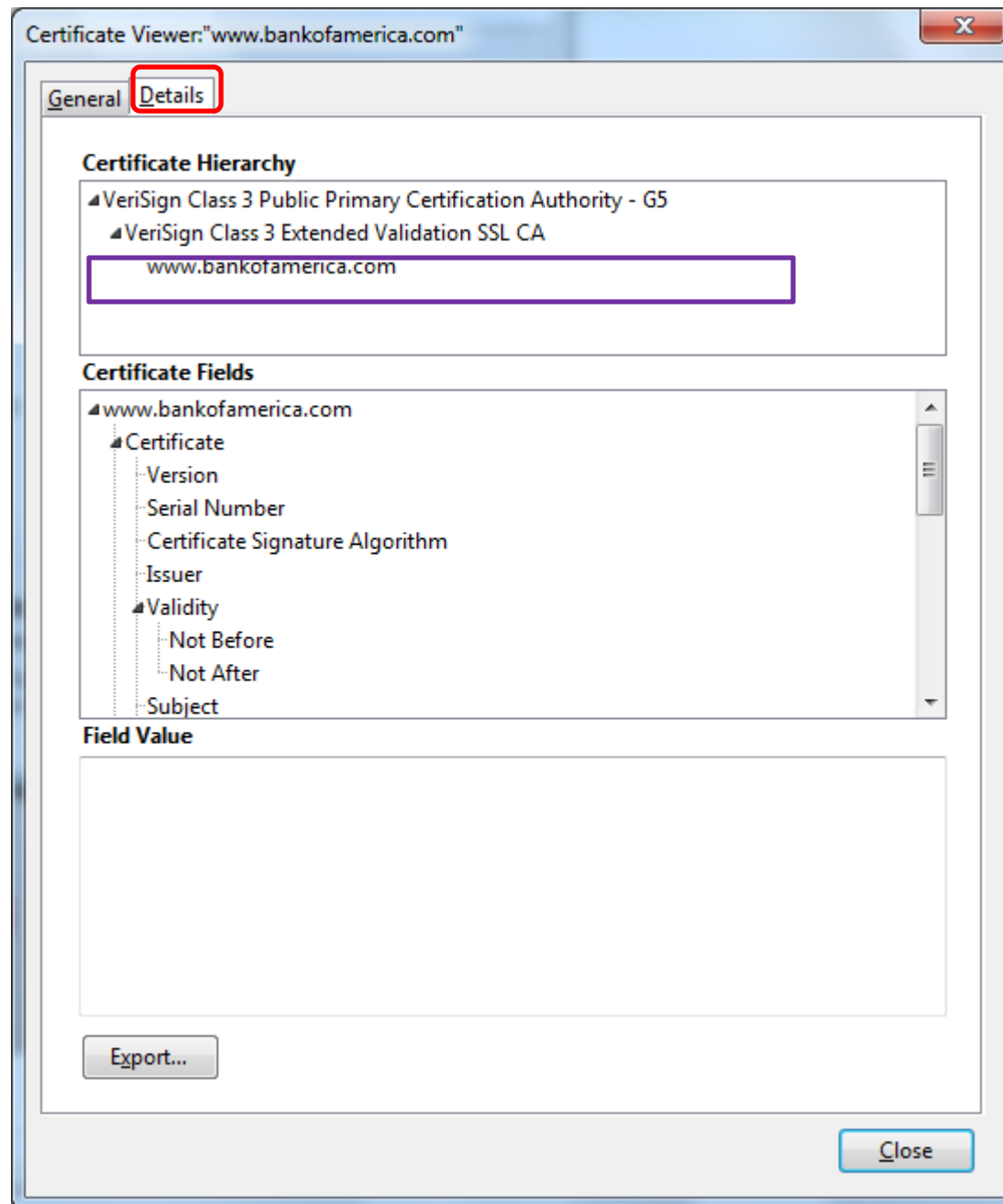
What is This?

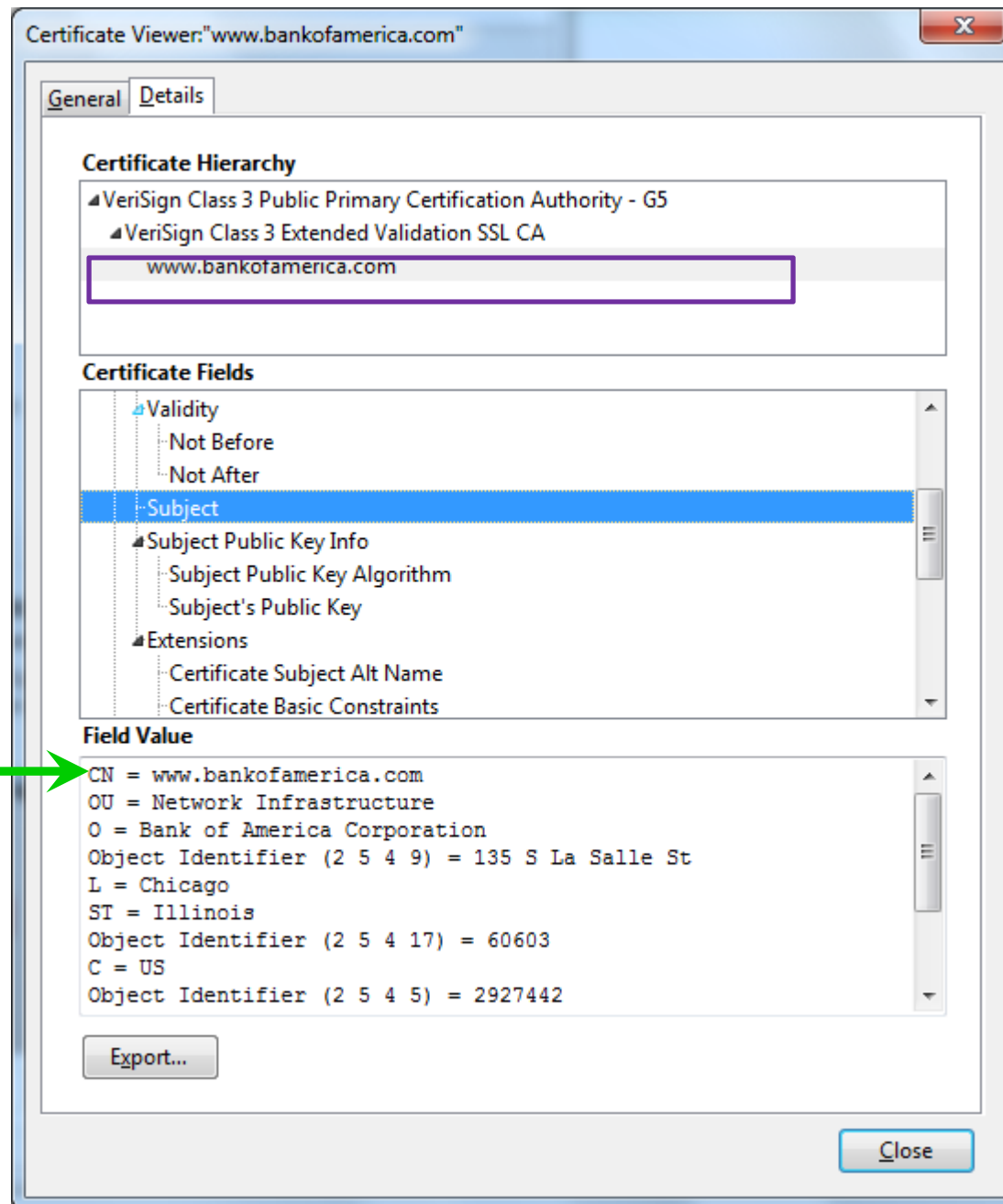


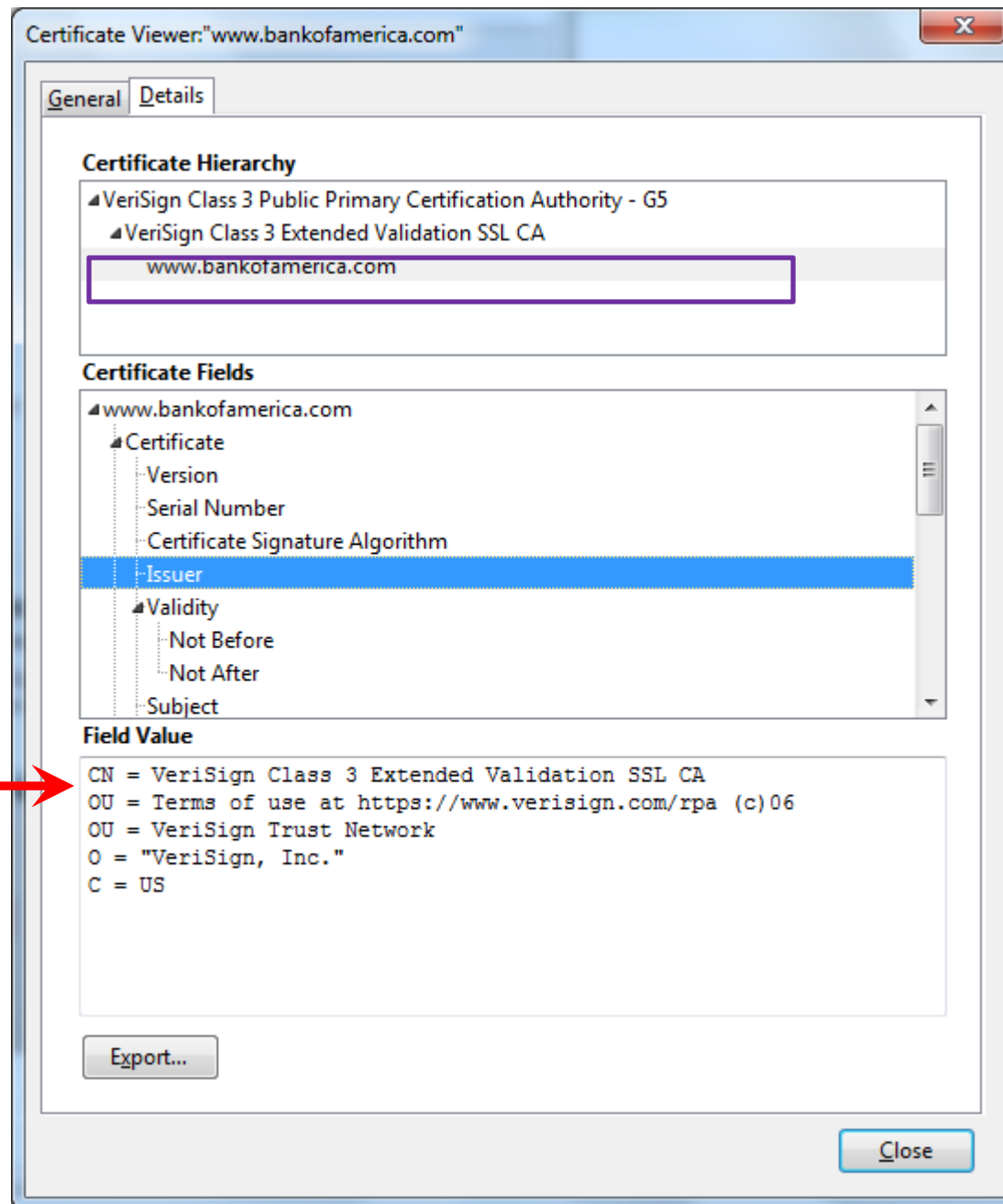


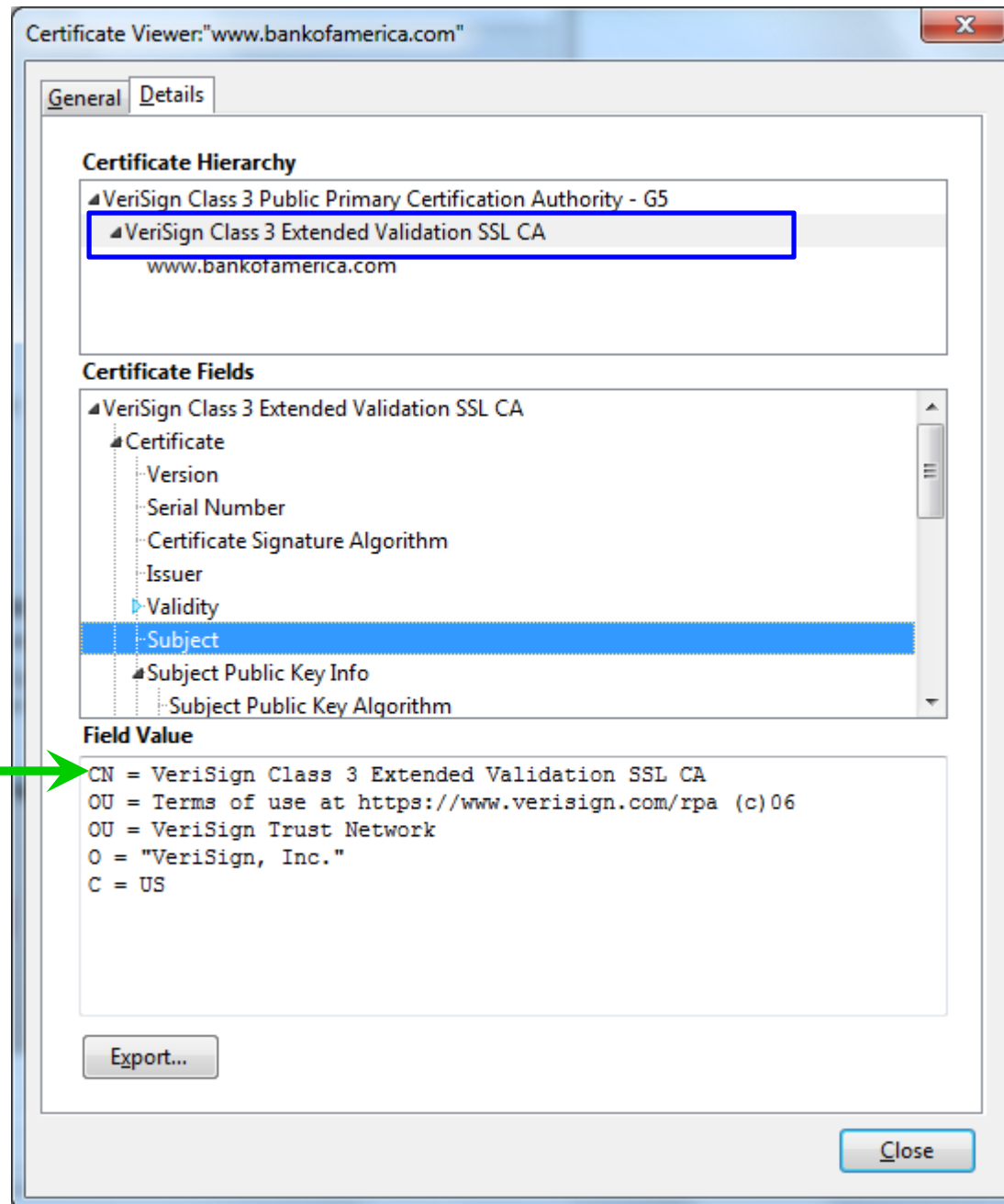


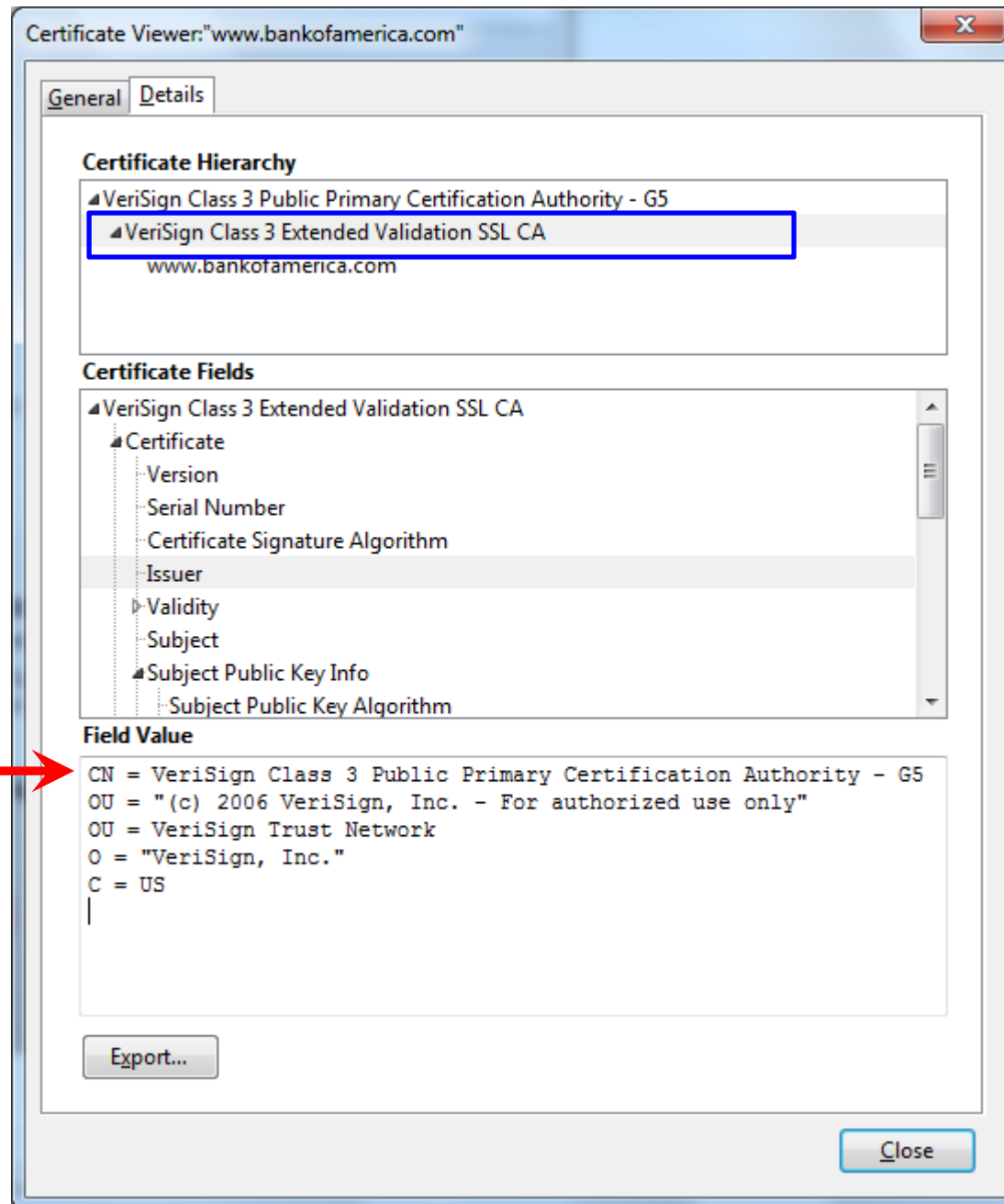


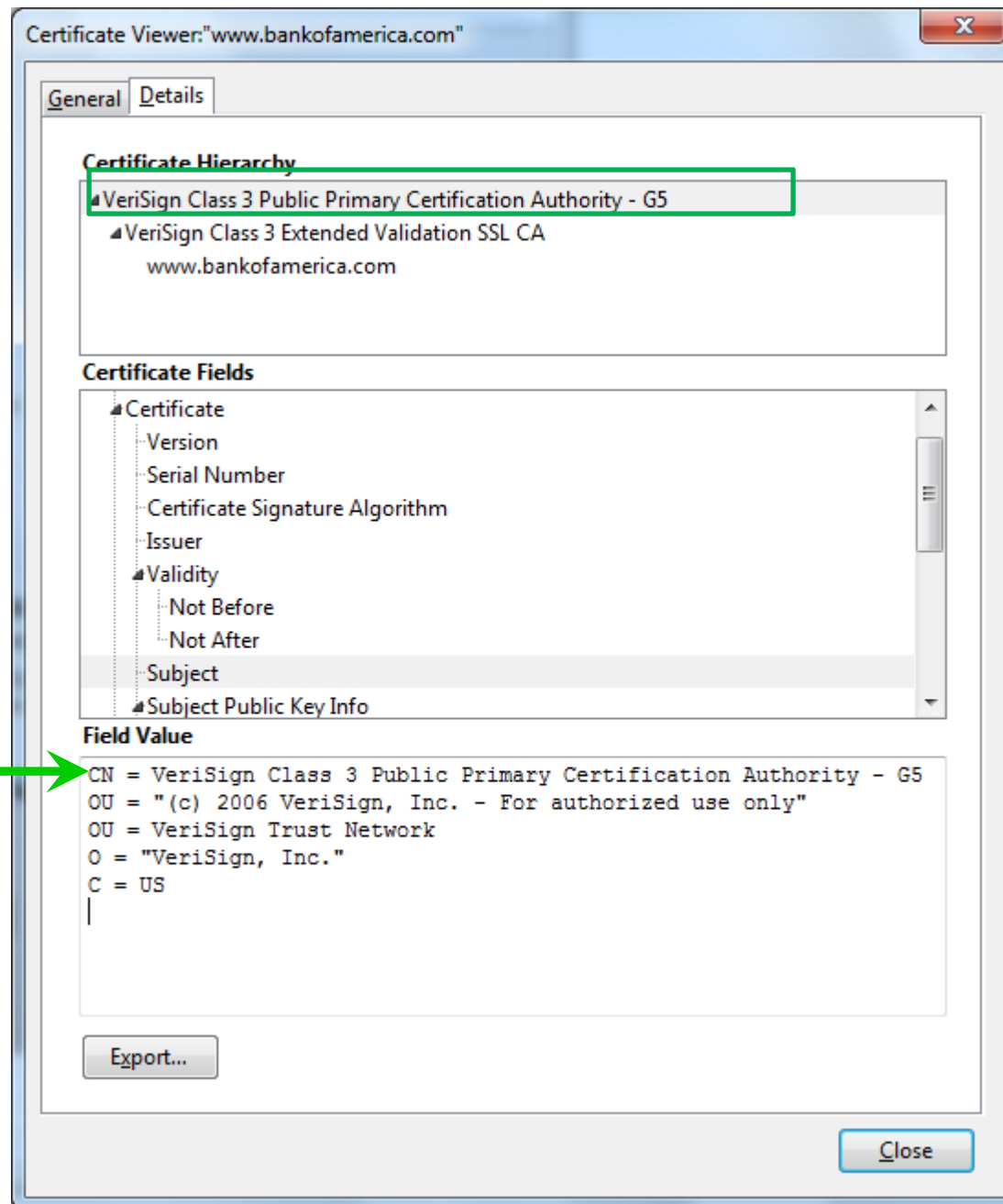


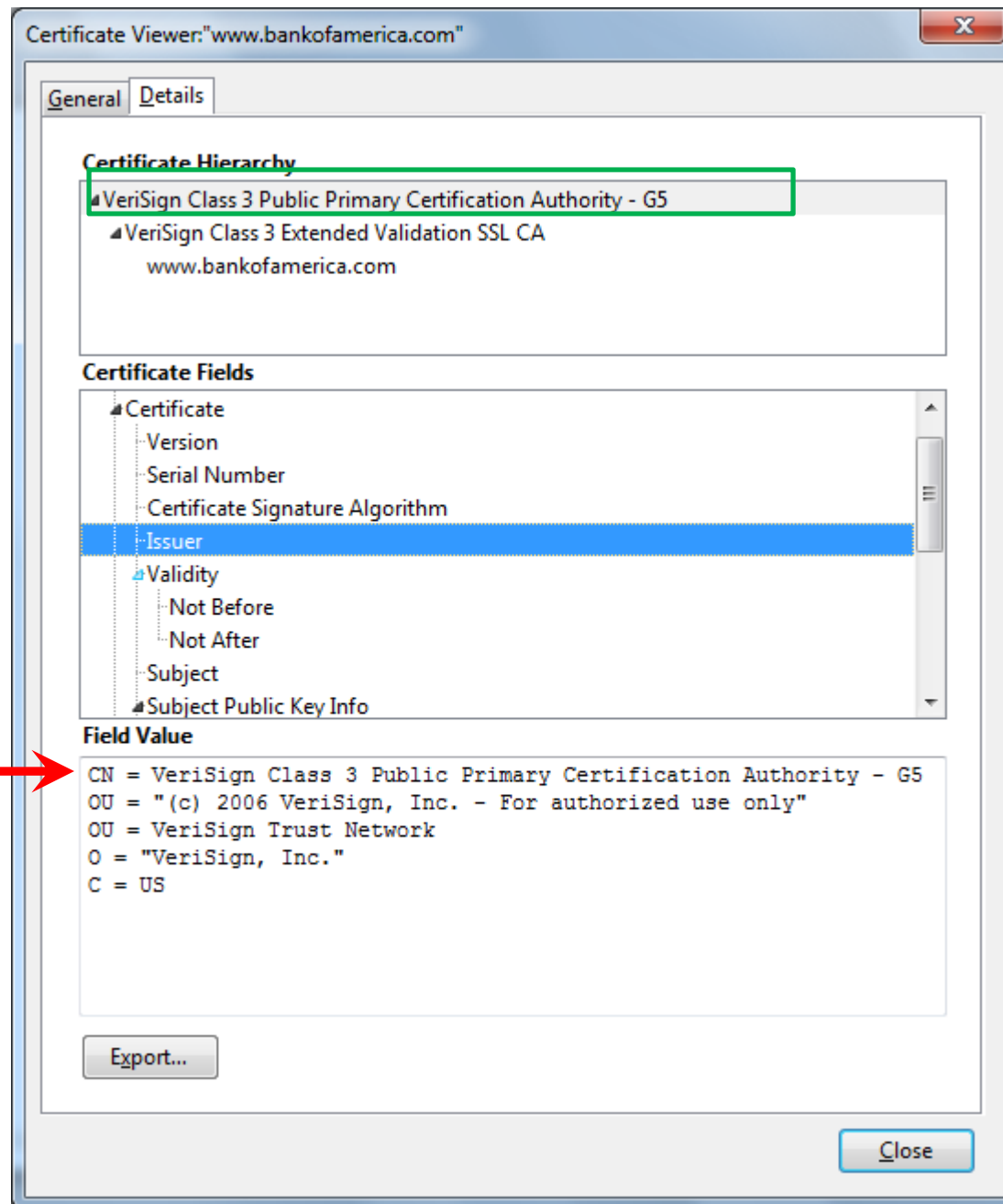


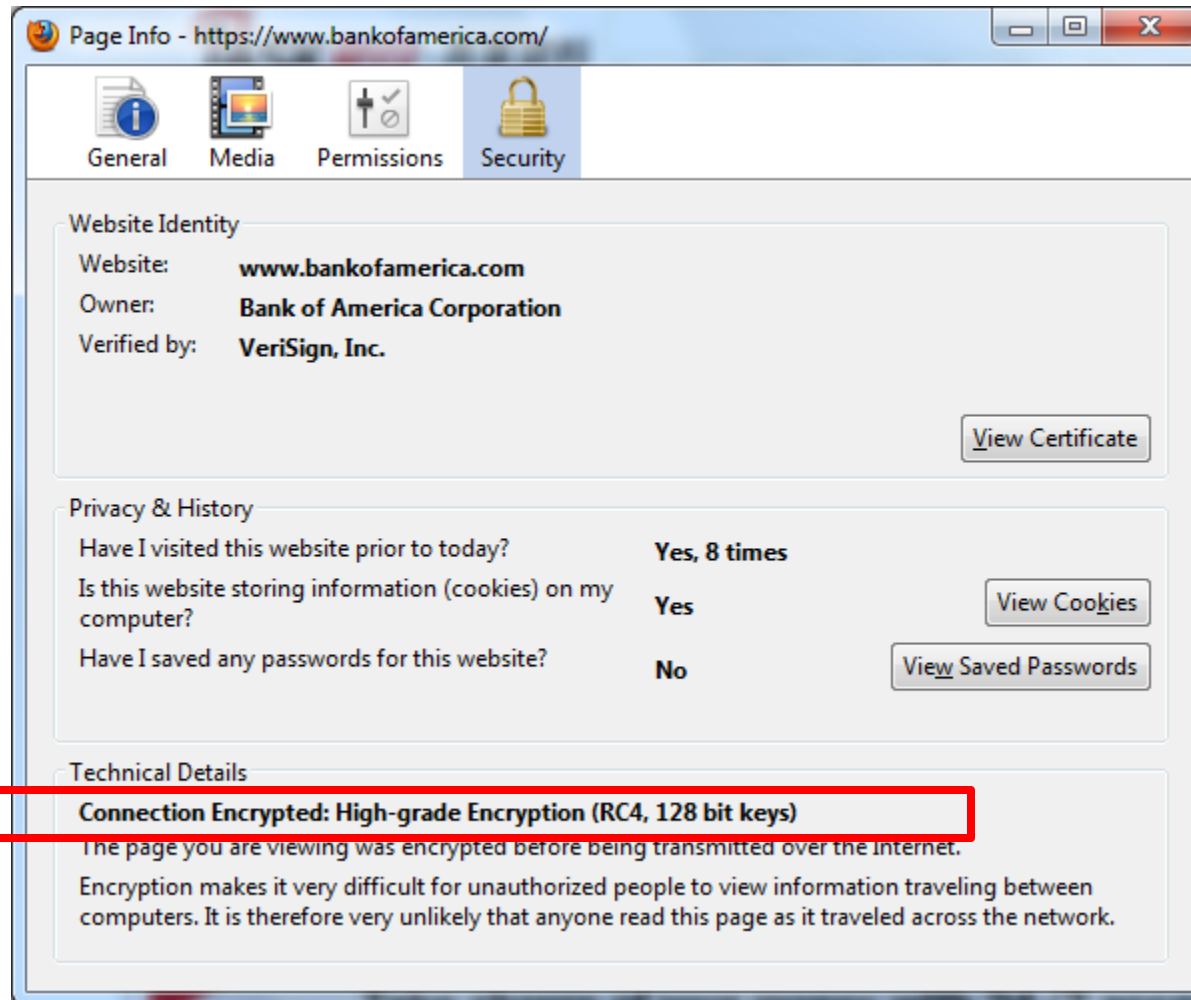


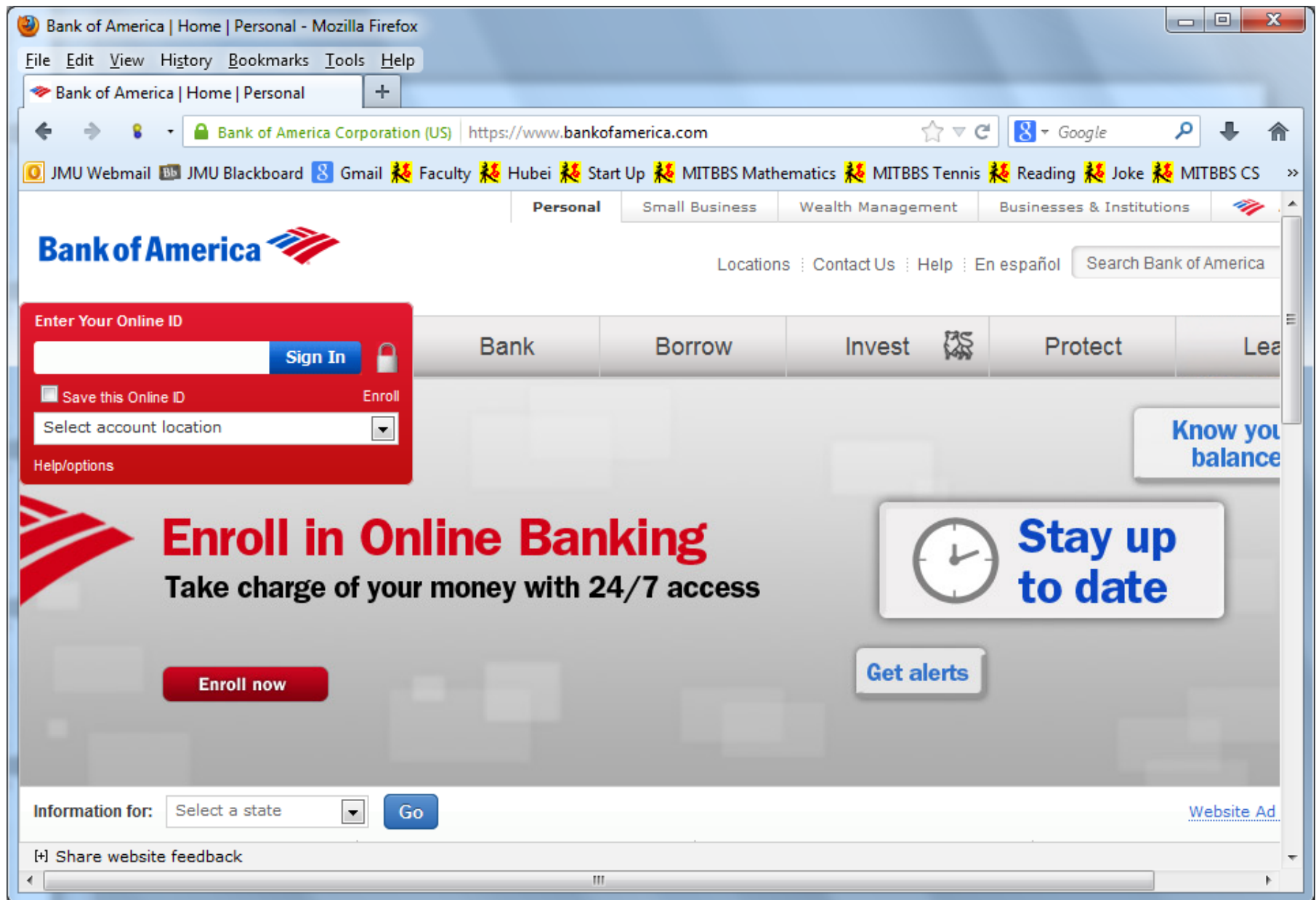


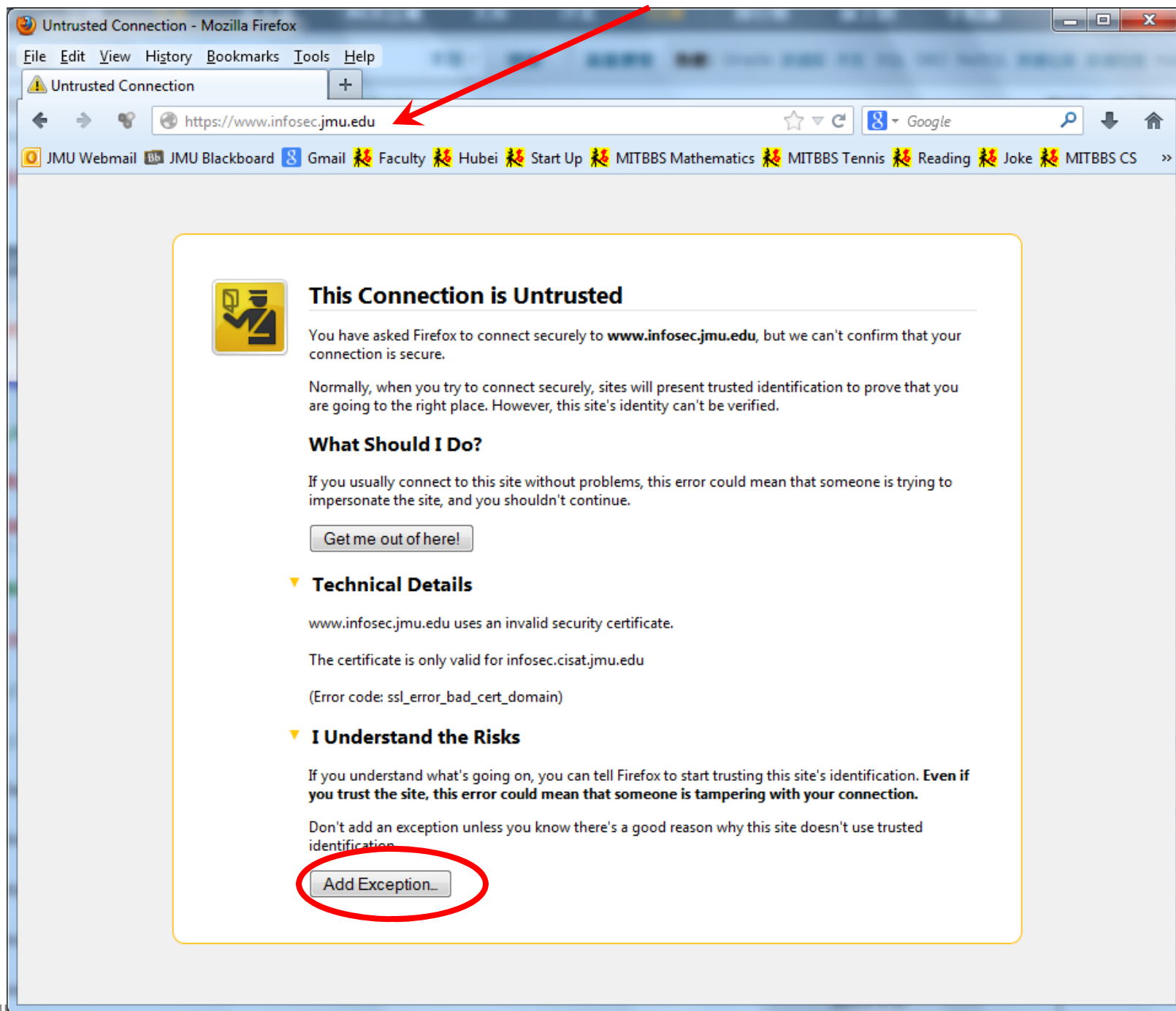


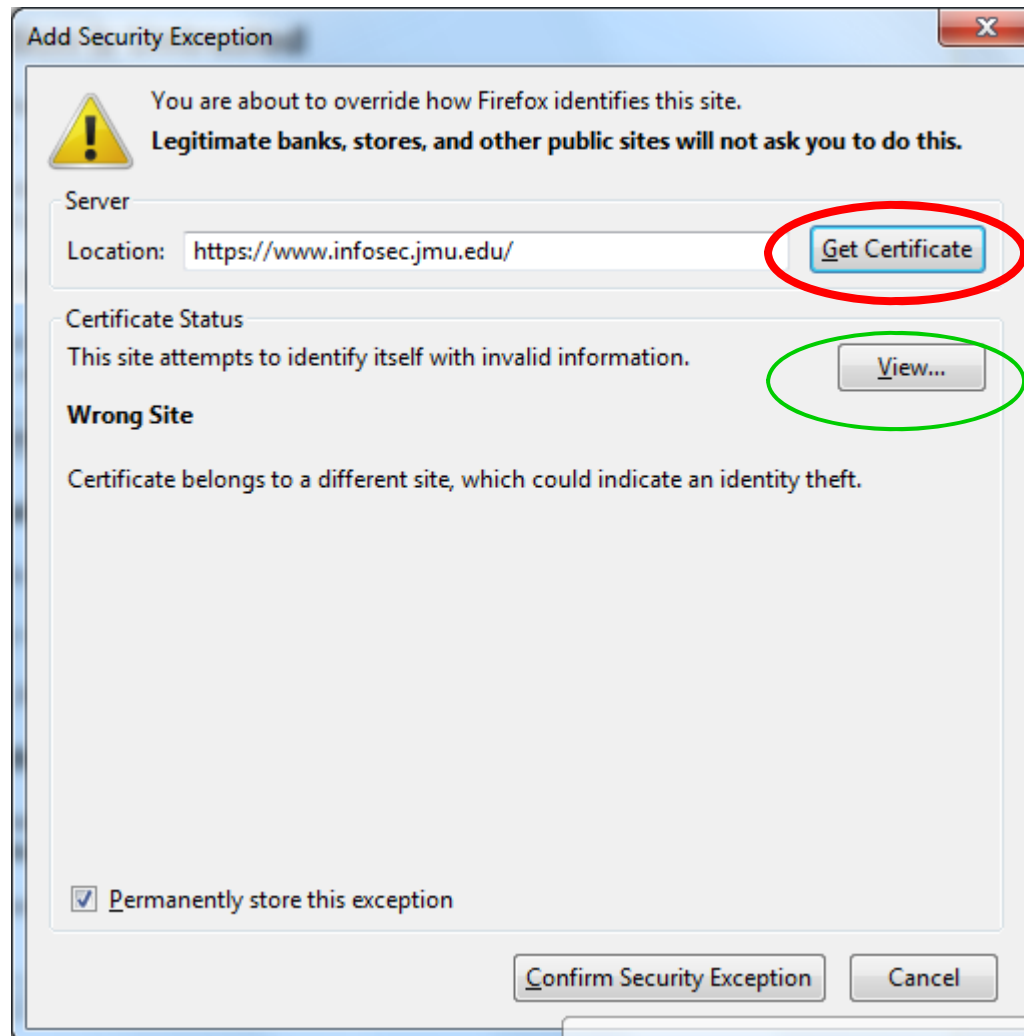


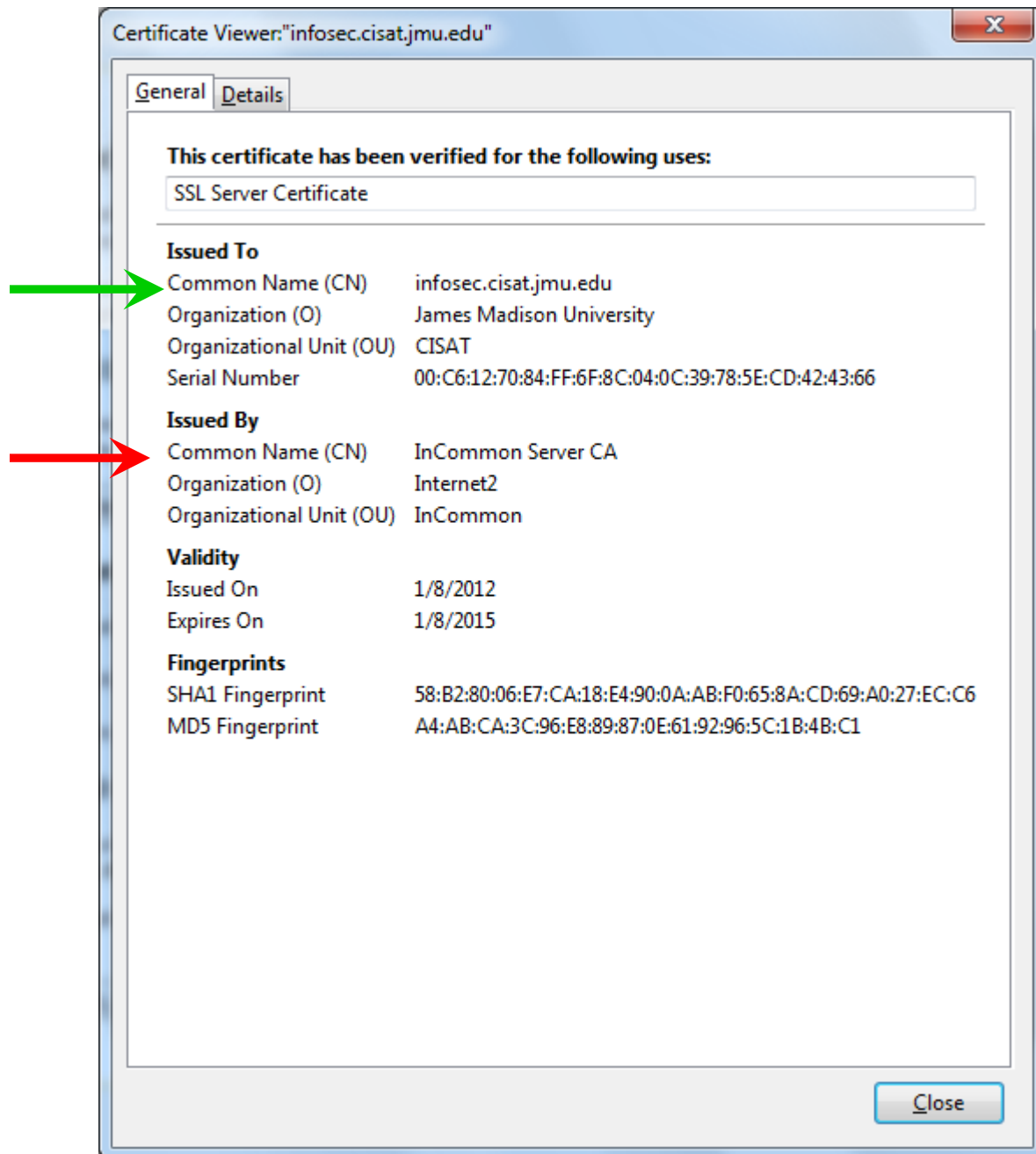


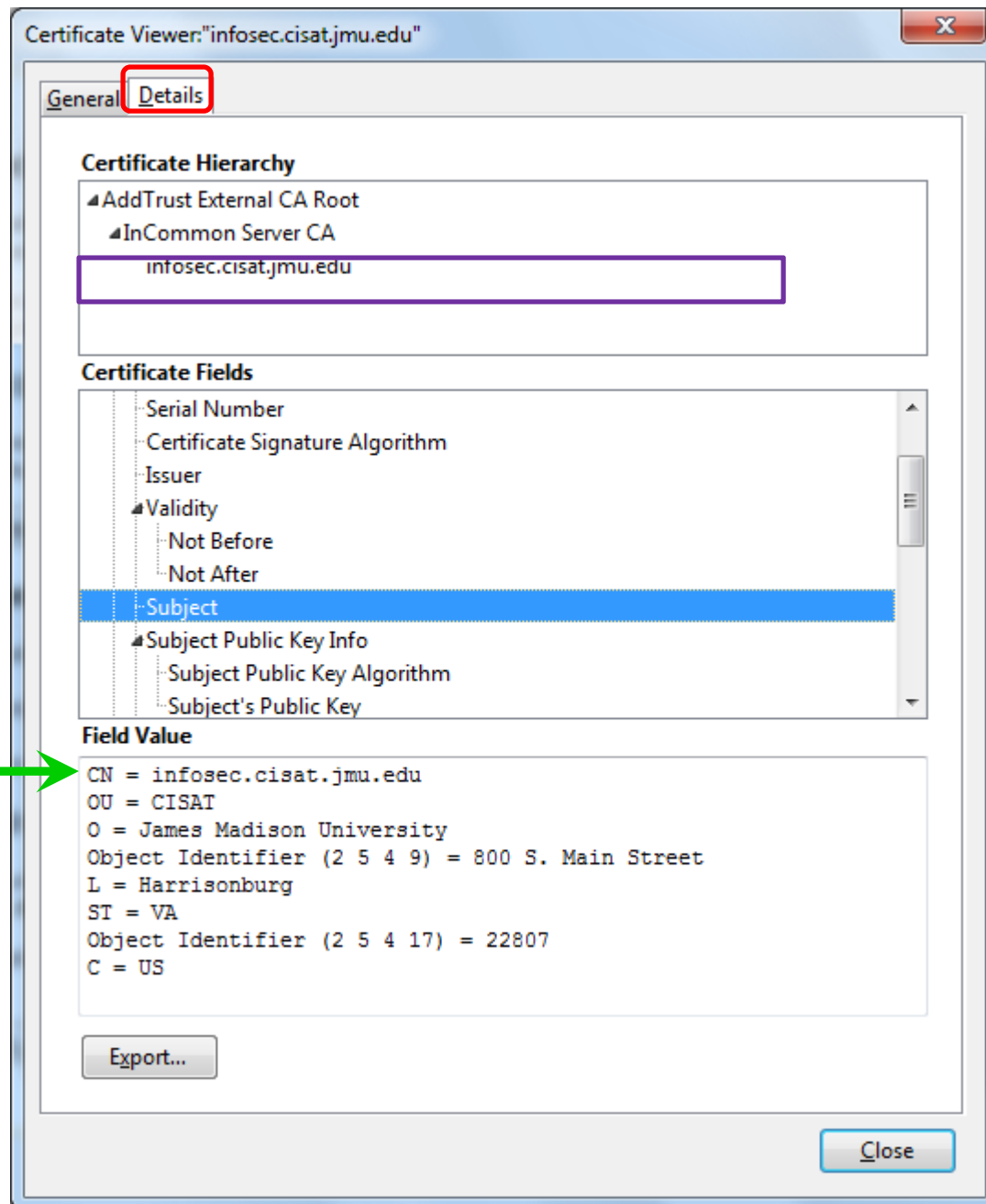


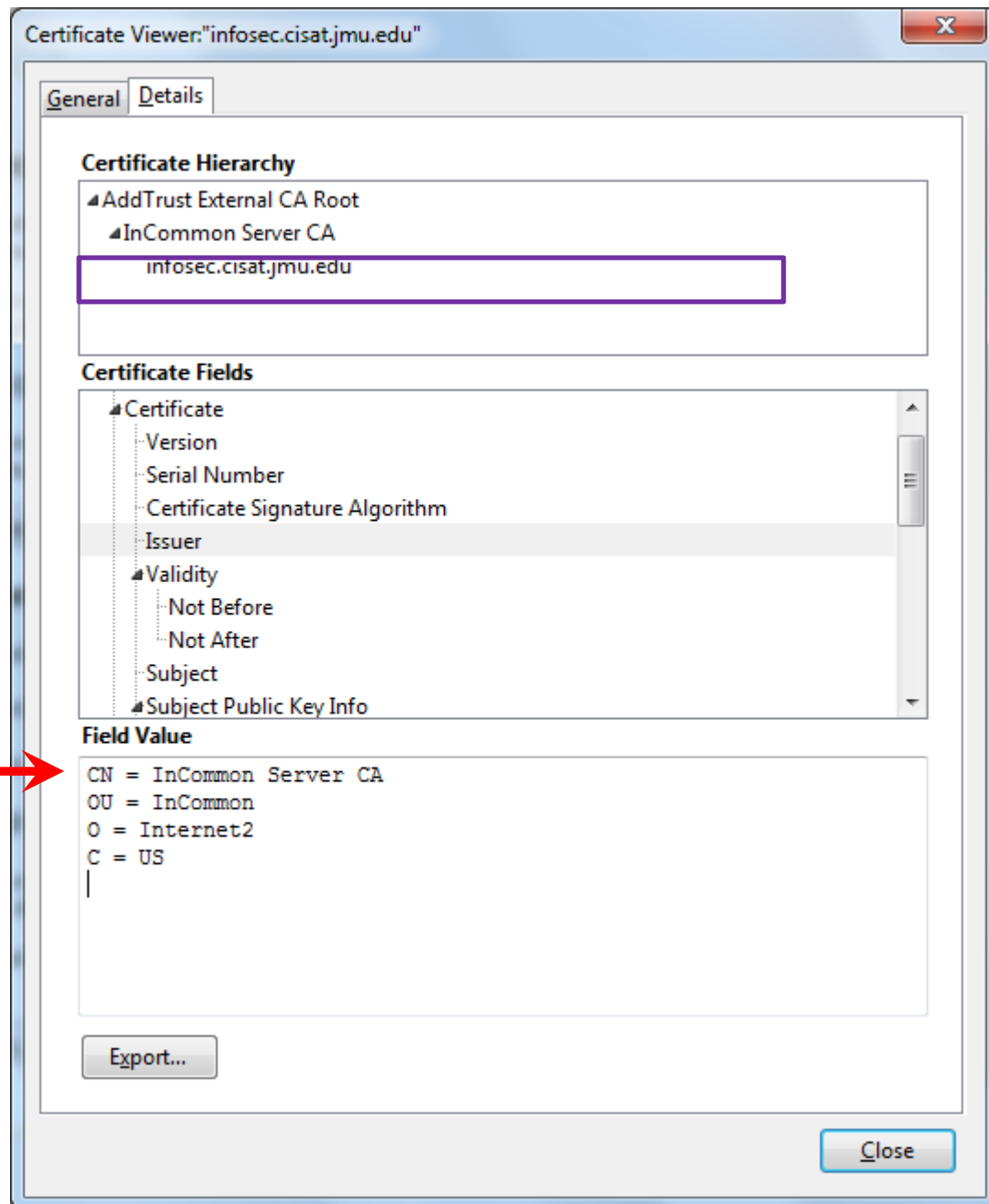


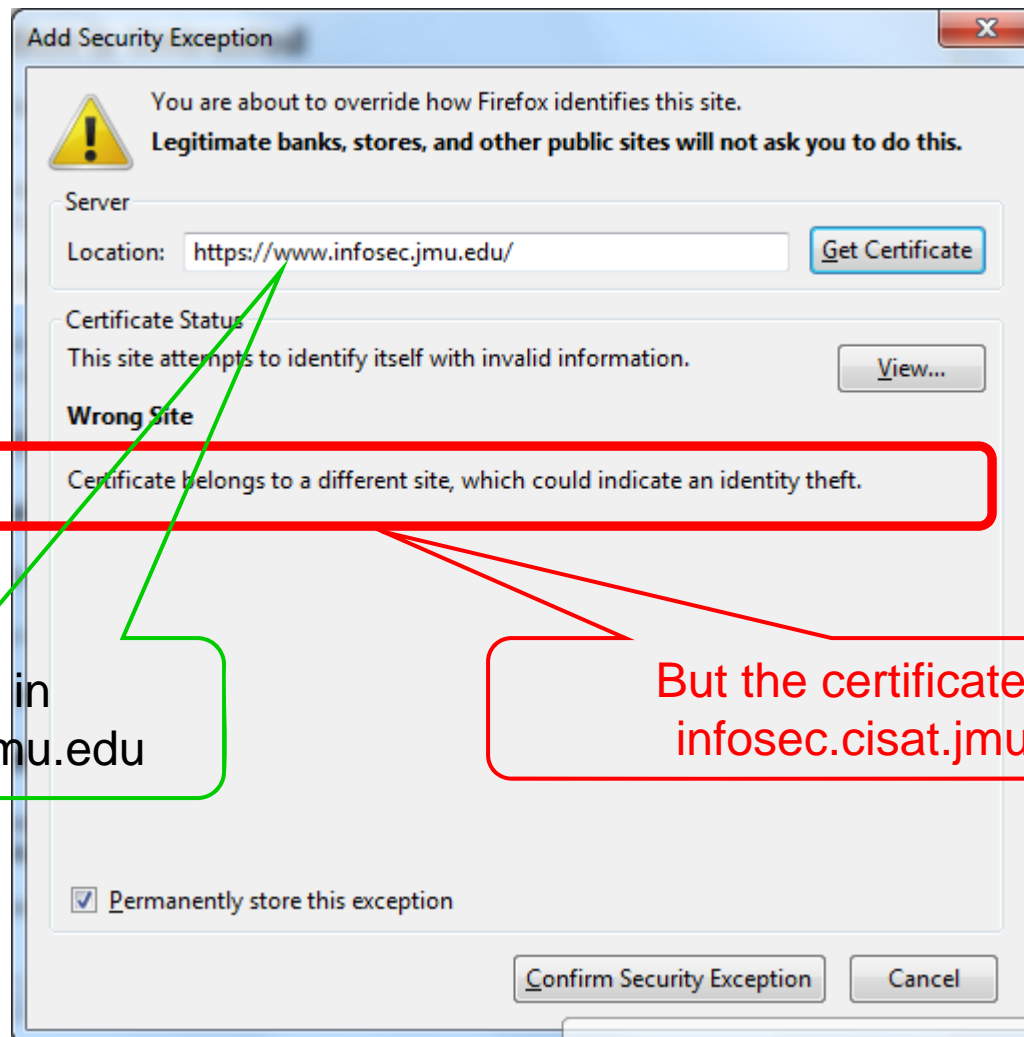












You typed in
www.infosec.jmu.edu

But the certificate is for
infosec.cisat.jmu.edu



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