# CS-627, Cryptology: Assignments

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#### <u>PART *I*</u>:

<u>Purpose</u>: (i) to Compile statistics on frequency of occurrence of individual letters and letter groups in a Text, and

(ii) to prepare a clean plaintext file from a crude source file for use as input to another program that will encrypt the text.

<u>Summary of Program Behavior</u>:

Queries the user to identify *which* file (Index Number) on which to operate.

Continually informs the user of the progress of program execution.

- Takes a text file as input whether ASCII or Unicode (either/or, doesn't have to handle both).
- Strips out non-alpha characters from the input text file, and outputs an all-lower-case alpha file for subsequent use as input to the <u>PART IIa</u> encryption program.

Counts the frequency of occurrence of each individual letter of plaintext.

- Counts the number of instances of every possible digram, trigram, tetragram, and pentagram.
- Produces a screen display <u>and</u> an output file reporting the statistical findings, as well as the date-and-time stamps of the program progress milestones.

#### PART I:

 Locate and compile text file groups from at least five distinct sources, such as: High-literary-quality news reports or essays (e.g., <u>New York Times</u>, especially the Sunday magazine section; <u>National Review</u>; <u>Wall Street</u> <u>Journal</u>)

Classical works of distinguished authorship (*e.g.*, Shakespeare, Melville, Stevenson, Poe, Clemens, Dickens, Tennyson)

- Scientific writing (e.g., <u>Scientific American</u>, <u>Science</u>, <u>Nature</u>, or a journal specific to some particular scientific discipline, such as <u>Journal of</u> <u>Physiology</u>, <u>Mathematical Gazette</u>, <u>Geographic and Global Issues</u> <u>Quarterly</u>)
- Computer Science (e.g., <u>IEEE Computer</u>, <u>Communications of the ACM</u>, <u>Dr.</u> <u>Dobbs' Journal</u>)

Other sources of distinctly different content

- (2) Each sample of text to contain <u>at least</u> 1,000 alphabetic characters.
- (3) Save the <u>original</u> source file in whatever form you found it, *e.g.*, .pdf, .doc, or .mht (except for .htm or .html documents, which you should save in .mht format).

PART *I* (continued):

(4) NAMING CONVENTIONS for DATA files (index n):

```
TEXT-SOURCE (for each textual source): source-n.htm, source-n.html,
                                       source-n.mht, source-n.pdf,
                                       source-n.doc, or whatever file type may
                                       be appropriate
INPUT: crude-plaintext-n.txt
                                    Includes formatting (line feed, tabs, etc.),
                                       indentation, spacing, non-alpha chars
OUTPUT<sub>1</sub>: processed-plaintext-n.txt
                                          Lower-case alphabetic characters
                                                exclusively; upper case
                                                converted to lower case, and
                                                everything else stripped off.
                                  Frequency of occurrence (%) for each letter
OUTPUT<sub>2</sub>: statistics-n.txt
                                  Number of instances of each non-zero-
                                       occurrence digraph
                                  Number of instances of each non-zero-
                                       occurrence trigraph
                                                                          4
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<u>PART I</u> (continued):

(5) NAMING CONVENTION for <u>PROGRAM</u> file:

crypto-project-part-I-yourJMUusername

For example, had I written the program: crypto-project-part-I-*abzugcx* 

<u>PART I</u> (continued):

(6) <u>Program Behavior</u> (not necessarily in chronological order):
 Queries the user for a two-decimal-digit <u>Index Number</u> (n).
 Measures and informs user of the size (number of characters) of the input file.
 Informs the user of current activity — updated every 5 seconds, and includes in each update message the current date and 24-hr-format time.

- Informs the user of major program milestones, via time-stamped messages output to the display, such as:
  - (a) Program starting to run (date, and time in 24-hr format).
  - (b) Generating an output file consisting of All-Lower-Case-Alpha (date-time).
  - (c) Completing the generation of the All-Lower-Case-Alpha processed-plaintext file (date-time).
  - (d) Beginning to Count the number of occurrences of the individual letters and letter groups (date-time).
  - (e) Completed the counting of letter and letter-group occurrences (datetime).
  - (f) Outputting the processed-plaintext file (date-time).
  - (g) Adding milestone-achievement information to the statistics file (date-time).
  - (h) Printing plaintext statistics and program execution information (date-time).

(h) Program operation successfully completed; exiting at: Date-Time.

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<u>PART I</u> (continued):

(7) <u>Specification for Content and Format of Statistical Output File</u>:

- (a) Name of INPUT file (*i.e.*, "crude-plaintext-*n*.txt").
- (b) Name of OUTPUT processed-plaintext file (*i.e.*, "processed-plaintext-*n*.txt")
- (c) Total number of characters in INPUT file.
- (d) Number of Alphabetic characters in both the INPUT and the OUTPUT files.
- (e) Letters in alphabetic order, with number and percentage occurrence of each (occurrences aligned on units digit, percentages calculated to precision of 0.01%, aligned on decimal point).
- (f) Digrams actually found, sorted into alphabetic order, with number of occurrences of each, aligned on units digit.
- (g) For <u>each</u> digram, show all trigrams found having the same starting characters and the number of occurrences of each. The trigrams should be indented so that they are shown to the right of the digram information, in the lines immediately below the digram.
- (h) Similarly for tetragrams and pentagrams.
- (i) A separate listing of all digrams and the number of occurrences of each, sorted in decreasing order of number of occurrences; same for trigrams, tetragrams, and pentagrams.
- (j) All of the milestones shown to the user during program execution.

<u>PART I</u> (continued):

Sample Output:

INPUT file: crude-plaintext-99.txt. OUTPUT file: processed-plaintext-99.txt

Total number of characters in INPUT file: 14,267 Number of Alphabetic characters present: 12,348

Occurrences in the plaintext of individual letters: a 1,017 8.23% b 185 1 49%

#### (continued)

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<u>PART I</u> (continued):

Sample Output

(continued):

Occurrences in the plaintext of letter groups (alphabetic order): 47 ab abd 12 abn 3 abo 21 9 abor 3 abori aborig 3 5 abort 8 an 6 ann ٠ • ٠

<u>PART I</u> (continued):

Sample Output

(continued):

30 Feb 2020, 0631 hrs: Program starting to run. 30 Feb 2020, 0642 hrs: Generating the processed-plaintext output file.

FURTHER INSTRUCTION:

You must also provide a narrative file (either .doc, .htm, or .pdf) describing the details of your approach. Your narrative should give an overview of how you tackled the problem, as well as a table listing all defined constants, all named variables, and all functions and classes that you originated. If the name of any of these items is less than fully evocative of its purpose, then add a brief explanation.

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File name: narrative-crypto-project-part-I-yourJMUusername.pdf © 2007 Charles Abzug

<u>PART II</u>: Vigenère Encryption and Decryption

- <u>Purpose</u>: (1) To encrypt a plaintext file using the Vigenère technique, based upon an encryption key supplied by the user.
  - (2) To decrypt a ciphertext file that had originally been encrypted using the Vigenère technique, based upon a decryption key supplied by the user.
- <u>PART IIa</u>: Vigenère <u>EN</u>cryption

#### Program Behavior:

- (1) Queries the user for the two-decimal-digit <u>Index Number</u> (n) associated with the plaintext message input: an ASCII text file composed ENTIRELY of lower-case Alpha characters (*i.e.*, one of the output-files from <u>PART I</u>).
- (2) Checks the user-specified file to see whether or not it meets the specified input conditions. If not, outputs to the user an appropriately-worded message, and then aborts.

<u>PART IIa</u>: Vigenère Encryption (continued)

- (3) Queries the user for a key word or key phrase, which MAY NOT include numerals, symbols or non-printing characters, BUT MAY include spaces and tabs, and may be of mixed case. If the user-supplied key word or key phrase does not meet the specification, outputs to the user an appropriately-worded error message, and then aborts.
- (4) Computes the EFFECTIVE Key-Word or Key-Phrase by converting the input to alllower-case and stripping off the second and subsequent appearances of any character present more than once in the input word or phrase.
- (5) Outputs the ciphertext in the form of an all-upper-case-alpha ASCII file (plus spaces and/or tabs, and carriage-returns and line-feeds or newline characters).

PART IIa: Vigenère Encryption (continued)

(6) NAMING CONVENTIONS for PROGRAM files:

(a) You will have <u>EITHER</u> one program that can do BOTH encryption & decryption, <u>OR</u> two programs, ONE for encryption and ONE for decryption.

(b<sub>1</sub>) Your choice: ONE program: crypto-project-part-II-*yourJMUusername* 

For example, had I written <u>one</u> program: crypto-project-part-II-*abzugcx* 

#### (b<sub>2</sub>) Alternative: TWO programs: crypto-project-part-II<u>A</u>-yourJMUusername (for ENcryption) and crypto-project-part-II<u>B</u>-yourJMUusername (for DEcryption)

For example, had I written <u>two</u> programs: crypto-project-part-II<u>A</u>-abzugcx and crypto-project-part-II<u>B</u>-abzugcx

PART IIa: Vigenère Encryption (continued)

(7) NAMING CONVENTIONS for DATA files (index n):

PLAINTEXT SOURCE (input file)	: processed-plaintext- <i>n</i> .txt (output from pt <i>I</i> ) Lower-Case Alphabetic characters exclusively; upper case has been converted by the <u>PART</u> <i>I</i> program to lower case, and everything else has been stripped off.
- •	Upper-Case alphabetic characters FIVE-character groups
	THREE-character space separating each pair of groups
	Length of each line <u>not to exceed</u> 80 characters
1	No partial blocks.
OUTPUT <sub>2</sub> : enciphering-info- <i>n</i> .tx	At Original user-supplied raw encryption key. Effective encryption key following processing.

<u>PART IIb</u>: Vigenère <u>DE</u>cryption

- (1) Queries the user for the two-decimal-digit <u>Index Number</u> (n) associated with the ciphertext message input: an ASCII text file composed ENTIRELY of fivecharacter blocks of upper-case Alpha characters, plus spaces and newline or carriage-return/linefeed characters.
- (2) Checks the user-specified file to see whether or not it meets the specified input conditions. If not, outputs to the user an appropriately-worded message, and then aborts.
- (3) Queries the user for a key word or key phrase, which MAY NOT include numerals, symbols or non-printing characters, BUT MAY include spaces and tabs, and may be of mixed case. If the user-supplied key word or key phrase does not meet the specification, outputs to the user an appropriately-worded error message, and then aborts.
- (4) Computes the EFFECTIVE Key-Word or Key-Phrase by converting the input to alllower-case and stripping off the second and subsequent appearances of any character present more than once in the input word or phrase.

PART IIb: Vigenère Decryption (continued)

- (5) Outputs the *plain*text in the form of an ASCII file.
- (7) NAMING CONVENTIONS for DATA files (index n):

CIPHERTEXT SOURCE (input file): ciphertext-n.txt (output from pt II) Upper-case alphabetic characters, plus spaces and linefeeds.

 OUTPUT<sub>1</sub>: deciphered-text-*n*.txt Lower-Case alphabetic characters: FIVE-character groups THREE-character space separating each pair of groups Length of each line <u>not to exceed</u> 80 characters No partial blocks.
 OUTPUT<sub>2</sub>: deciphering-info-*n*.txt Original user-supplied raw decryption key. Effective decryption key following

processing.

PART IIb: Vigenère Decryption (continued)

FURTHER INSTRUCTION:

You must also provide a narrative file (either .doc, .htm, or .pdf) describing the details of your approach. Your narrative should give an overview of how you tackled the problem, as well as a table listing all defined constants, all named variables, and all functions and classes that you originated. If the name of any of these items is less than fully evocative of its purpose, then add a brief explanation.

File name: narrative-crypto-project-part-II-yourJMUusername.pdf

<u>PART III</u>: Cryptanalysis of a Vigenère Encipherment

<u>Purpose</u>: To cryptanalyze a Vigenère-encrypted ciphertext, recovering the effective key originally used to encrypt the plaintext (*i.e.*, the original key with duplicate letters stripped off), as well as the plaintext.

Program Behavior:

- (1) Calculates the overall Index Of Coincidence (*IOC*) of a Vigenère–encrypted ciphertext.
- (2) Determines the effective length of the Vigenère encryption key; two suggested approaches:
  - (a) Use the mathematical formula derived by William Friedman to calculate a best estimate of keylength, and then try out several nearby values looking for best fit. (The "educated guess" method)
  - (b) Try <u>all</u> possible values of effective keylength from 2 through 26, calculating for each possible keylength value the IOC for each monoalphabetic substitution, and looking for the keylength value that gives the best fit. (The "brute force" method)

PART III: Cryptanalysis of a Vigenère Encipherment (continued)

(3) Outputs two files:

OUTPUT<sub>1</sub>: cryptanalytic-progression-*n*.t×t shows the steps taken and each successive calculation performed, *e.g.*:

> Trying keylength 4. IOC = 4.73, 4.94, 4.47, 4.69Trying keylength 5. IOC = 4.99, 5.23, 5.14, 4.83, 5.08

FINAL KEYLENGTH = 10 EFFECTIVE KEYWORD = hieronymus

OUTPUT<sub>2</sub>: recovered-plaintext-n.txt

shows the Vigenère decryption of the cryptanalyzed ciphertext using the effective keyword

<u>PART III</u>: Cryptanalysis of a Vigenère Encipherment (continued):

(4) NAMING CONVENTION for <u>PROGRAM</u> file:

crypto-project-part-III-yourJMUusername

For example, had I written the program: crypto-project-part-III-*abzugcx* 

FURTHER INSTRUCTION:

You must also provide a narrative file (either .doc, .htm, or .pdf) describing the details of your approach. Your narrative should give an overview of how you tackled the problem, as well as a table listing all defined constants, all named variables, and all functions and classes that you originated. If the name of any of these items is less than fully evocative of its purpose, then add a brief explanation.

File name: narrative-crypto-project-part-III-yourJMUusername.pdf

<u>PART IV</u>: Rivest-Shamir-Adelman (*RSA*) encryption and decryption

<u>Purpose</u>: (1) To generate a pair of prime numbers, p and q;

- (2) To make use of the two primes to generate a pair of *RSA* keys, one private and the other public, and finally
- (3) To use the two keys to encrypt and decrypt a plaintext message.

PART IVa: Generation of an RSA Key Pair

Program Behavior:

- (1) Generates a random number of 32-bit length: p.
- (2) Tests the number for primality:
  - (a) "Sieve of Eratosthenes"
  - (b) Fermat Test.

NOTE: There may be other primality-testing techniques that are practicable for 32-bit primes, but for this exercise you should use a technique that is

<u>PART IVa</u>: Generation of an RSA Key Pair (continued):

readily extensible for use with 512-bit primes. Thus, for example, with a 32bit randomly-generated number, it may be practical to test for primality by dividing the number by all known primes up to 16 bits in length. However, since this technique cannot be extended to 512-bit numbers, you should not use it.

(3) Repeats steps 1 and 2 to produce a second 32-bit prime: q.

- (4) Defines the first member of an RSA key pair, a public key, as the pair of numbers consisting of:
  (a) The 4<sup>th</sup> Fermat number: 2<sup>16</sup> + 1
  (b) n = p q
- (5) Applies the Extended Euclidian Algorithm to the 4<sup>th</sup> Fermat number to obtain its multiplicative inverse modulo  $(p 1) \cdot (q 1)$

<u>PART IVa</u>: Generation of an RSA Key Pair (continued):

- (6) Defines the second member of the *RSA* key pair, the private key, as the pair of numbers consisting of:
  - (a) The multiplicative inverse of the 4<sup>th</sup> Fermat number, obtained in the previous step.

(b)  $n = p \bullet q$ 

(7) Data Output Files: each an ASCII file consisting of two lines: exponent in first line, modulus in second line.

RSA-private-key-*yourJMUusername* RSA-public-key-*yourJMUusername* 

(8) FILE NAMING CONVENTIONS for <u>PROGRAM</u> file:

crypto-project-part-IVa-yourJMUusername

For example, had I written the program: crypto-project-part-IVa-*abzugcx* 

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#### PART IVD: RSA Encryption and Decryption

Program Behavior: ENCRYPTION MODE

- (1) Queries the user for the two-decimal-digit <u>Index Number</u> (n) associated with the plaintext message input: an ASCII text file composed ENTIRELY of lowercase Alpha characters (i.e., one of the output-files from <u>PART I</u>).
- (2) Checks the user-specified file to see whether or not it meets the specified input conditions (see <u>PART I</u>). If not, outputs to the user an appropriately-worded message, and then aborts.
- (3) Pads the plaintext file to a multiple of the 32-bit block size to be used for RSA encryption, using one of the padding algorithms described in Fergusson and Schneier's Practical Cryptography.
- (4) Queries the user for the file-identifier of a file holding one key of a matched *RSA* key pair.

PART IVD: RSA Encryption and Decryption: ENCRYPTION MODE (continued)

- (5) Takes each block of the padded plaintext file, and encrypts it using the specified key. Do NOT use a built-in exponentiation function to accomplish the encryption. Instead, utilize the algorithm shown in class, successively squaring the 32-bit plaintext block and then immediately reducing the product by the modulus *n*. Once you have produced all of the squares up to the highest degree necessary, then multiply the individual values together one pair at a time and do a modulo *n* reduction each time.
- (6) Deposit the ciphertext blocks in the output file. Note that the output file should be a binary or hex file, since there is no guarantee that the process of exponentiation will result in printable ASCII characters.
- (7) NAMING CONVENTION FOR DATA OUTPUT FILE:

RSA-encrypted-ciphertext-n.bin

PART IVD: RSA Encryption and Decryption

Program Behavior: DECRYPTION MODE

- (1) Queries the user for the two-decimal-digit <u>Index Number</u> (*n*) associated with the *RSA*-encrypted ciphertext file.
- (2) Queries the user for the file-identifier of a file holding one key of a matched *RSA* key pair. This file must contain the companion key to the one that had been used for the encryption.
- (3) Decrypts the file using the identical mathematical procedure that had been used to encrypt it, except for the difference in key.
- (4) Removes the padding that had augmented the plaintext file immediately prior to encryption.

PART IVD: RSA Encryption and Decryption: DECRYPTION MODE (continued)

(5) Writes the decrypted and pad-free plaintext into an ASCII text file.

(6) NAMING CONVENTION FOR DATA OUTPUT FILE: RSA-decrypted-n.txt

FURTHER INSTRUCTION:

You must also provide a narrative file (either .doc, .htm, or .pdf) describing the details of your approach. Your narrative should give an overview of how you tackled the problem, as well as a table listing all defined constants, all named variables, and all functions and classes that you originated. If the name of any of these items is less than fully evocative of its purpose, then add a brief explanation.

File name: narrative-crypto-project-part-IV-yourJMUusername.pdf

#### END