Introduction and Overview:

Mathematics can be divided into two realms, the realm of continuous entities and the realm of discrete entities. The digital computer, by the very nature of the way it is constructed, models the world as a collection of discrete rather than continuous objects. Discrete structures are abstract mathematical concepts that are employed in the description and representation of discrete objects, as well as of the relationships between them. It is vitally important that the modern computer scientist be well-versed in the various sub-branches of mathematics that are concerned with the use, treatment, and manipulation of discrete structures.

Summary Course Description:

Counting and Probability; Functions; Recursion; Efficiency of Algorithms; Relations; Regular Expressions and Finite-State Automata.

Course Outline:

1. Counting and Probability
   a. Definition: Sample Space
   b. Definition: Outcome
   c. Definition: Event
   d. The simplifying assumption of Equal Likelihood of all possible outcomes
   e. Lists, List Elements, and Sublists
   f. One-Dimensional Arrays
   g. Possibility Trees
   h. Multiplication Rule
   i. Permutations
   j. Addition Rule
   k. Difference Rule
   l. Inclusion/Exclusion Rule
   m. r-Combinations
   n. Ordered Selections
   o. Unordered Selections
   p. Relation between Permutations and Combinations
CS-228: Discrete Structures II Syllabus

q. Permutation with Repetition
r. \(r\)-Combinations with Repetition
s. Multisets
t. Combinatorial Formulae
u. Pascal’s Triangle
v. The Binomial Theorem
w. Probability Axioms
x. Expected Value
y. Conditional Probability
z. Bayes’ Theorem
aa. Independent Events

2. Digital Logic
   a. Logic Gates and Circuits
   b. Flip-Flops

3. Representation of Integer and Non-Integer Numbers
   a. “Unsigned” Numbers
   b. Ones’-Complement
   c. Two’s-Complement
   d. Signed-Magnitude
   e. Saturation Arithmetic
   f. Floating-Point Representation

4. Logic Part II
   a. Review of Logic Part I from CS-227
      i. Truth Tables
      ii. Conjunction, Disjunction, Negation, Implication
      iii. Hypothesis, Conclusion, Converse, Inverse, Contrapositive
      iv. DeMorgan’s Laws
      v. Natural Deduction: Modus Ponens, Modus Tollens, etc.
      vi. Universal Quantification and Existential Quantification
      vii. Validity & Implication
   b. Natural Deduction
   c. Consistency and Completeness
   d. Normal Forms (conjunctive and disjunctive)

5. Graphs and Trees
   a. Introduction to Graphs
   b. Paths and Circuits
   c. Directed and Undirected Graphs
   d. Cyclic and Acyclic Paths
   e. Trees
   f. Spanning Trees
   g. Traversal Strategies

6. Proof Techniques: Induction on Graphs

7. Finite-State Automata
   a. Definition of a Finite-State Automaton
   b. State Diagrams
c. The Finite State Machine as a Virtual Machine  
d. The Finite State Machine as a Representation of Computation  
e. Limits of Deterministic Finite State Machines

Course Objectives:

By the end of the course, the student should be able to:

a. Apply the principles of counting to evaluate the number of combinations or the number of permutations appropriate to a particular situation.

b. Calculate the probability of occurrence of some event, under the assumption of equal likelihood of all possible outcomes.

c. Calculate the probability of occurrence of some event in the situation where all possible outcomes are not equally likely.

d. Calculate the value of a binomial expression.

e. Determine the degree of a graph.

f. Understand the relationship between a graph and its matrix representation.

g. Determine whether two automata are or are not equivalent.

Textbooks and Other Source Materials:

Main Course Textbook (REQUIRED):


RECOMMENDED:

Course Practices:

**Attendance Policy, and Relationship of Course Sessions to Readings:** In class, announcements are sometimes made of new or changed course policies, requirements, modifications to assignments, etc. Information provided in such announcements might not appear anywhere in the course documentation. Furthermore, course sessions will cover some of the material in the readings, but will also include some material not covered by the readings. Therefore, students must not only do all of the readings, but must also attend all classes.

Normally, there are only three acceptable grounds for a student’s missing a class: (1) grave medical or (2) serious personal problems affecting the student him/herself, or in some cases affecting a member of the student’s immediate family. The other acceptable excuse for a student’s missing a class is (3) force majeur (overpowering force due to an unexpected and uncontrollable event). An example of force majeur is the occurrence of a flat tire or of a motor vehicle accident involving your vehicle while you are traveling to class. If you want to claim exemption on one of these three grounds, be prepared to submit evidence (e.g., a note from a licensed physician on the physician’s stationery, or a copy of an official police accident report).

Attendance is normally taken at every class. Your presence in class does not get factored directly into the grading process. Why, then, is attendance taken? The purpose is three-fold: (i) attendance data sometimes provide me with advance information that a student may be experiencing academic difficulty because of medical or personal problems, or for some other reason. In addition, (ii) I may also consult attendance records in deciding how much I am willing to extend myself in providing help should you get into academic difficulty during the semester. You are in a much better position to get a “break” if you have been conscientiously attending class. Note, however, that I do reserve the right to reduce a student’s grade if he/she either has an excessive total number of unexcused absences (four or more), or is absent on the class day immediately before or immediately after an official university holiday, or whose classroom behavior is disruptive.

Note that if you do miss out on a class, it is your responsibility to find out what we covered in class, as well as what announcements might have been made. It is also your responsibility to obtain the missed material. “I wasn’t in class when you made that announcement” is not an acceptable excuse for your failure to comply with any directives issued in class. Please see the companion to this section entitled, “Policy Regarding Classes Missed by Students”.

**E-mail on Course-Related Matters:** All E-mail messages related to the course must be identified by a Subject header that begins by identifying the course and section about which the body of the message is concerned.

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1 Immediate family, as defined for the purpose of this policy, consists of your father/grandfather, mother/grandmother, sister, brother, spouse, or fiancé to whom you are formally engaged. Please NOTE that as far as I am concerned, your girlfriend/boyfriend is not a member of your immediate family.
Format for Submitted Homeworks: Submitted homeworks are required to be of the following form in order for you to receive credit:

1. Your name must appear legibly in the top left corner of the first page and of all odd-numbered pages.
2. On the first page only, following your name, you must write the course number: CS-228.
3. Next, there must be a declaration of compliance with the JMU Honor Code, including your signature.
4. On the first page only, in the center of the page near the top, you must prominently write: Assignment # _____ (fill in the assignment number); Chapter # _____ (fill in the chapter number).
5. Each numbered problem must start on a new line, with the number of the problem clearly identified at the beginning of the line.
6. Skip two lines or more after each problem.
7. Write your solutions legibly.
8. Fasten the pages together by stapling them in the upper left-hand corner. Paper clips or dog-ear of the pages is NOT acceptable in lieu of a staple. Please note that if you cannot afford to buy a stapler, or if you have a stapler but forget to bring it with you, there are several staplers available for student use in the CISAT Copy Center in Room 1002. There is no charge for use of the Copy Center’s staplers.
9. Bring the completed assignment in to class on the date that it is due, and be prepared to submit it at the beginning of class.

Grading of Tests and Assignments, and the JMU Honor Code: You will eventually be assigned an overall course grade. The course grade will be based principally upon your performance on quizzes, exams, homework assignments, projects, etc. Integrity of the grading process requires that you be graded on the basis of your own work, and not on someone else’s. Yet, sometimes you may get stymied and not be able to complete an assignment on your own. If you find it necessary to obtain help from someone else in completing your assignment, you are required to indicate that by clearly marking it on your assignment. Thus, if one of your colleagues contributes a line of code to your computer program, you should plainly mark that via a comment inserted into the text of the program, as in the following example:

//Hieronymous Johnson kindly contributed the following line of code to my program:
for (int i=0, k=4-i; i<10; k=Math.abs(4++1+(i>4?1:0)));

Similarly, non-programming assignments should be clearly footnoted or annotated to indicate where someone else’s help contributed to the product. In the absence of a clear annotation in your submitted assignment, you will be assumed to be the sole author of all work that you submit. Should that turn out not to be the case, it will be accounted as an honor code violation and will be dealt with severely. Details of the JMU Honor Code are to be found at: http://www.jmu.edu/honor/

2 I am indebted to Prof. David Brunner for contributing the coding example shown above.
Honor Code: The JMU Honor Code specifies that every assignment, whether written or electronically submitted by a student, is submitted pursuant to the Honor Code, and must contain a declaration stating that “This work complies with the JMU Honor Code.”, together with your signature. For this course, it is required that you place this signed declaration on the first page of your assignment. If the Honor Code declaration is not included at the time that the assignment was submitted, your grade for that assignment will be a zero. It is your responsibility to see to it before submitting your work that your signed Honor Code declaration is easily found on the first page of your assignment. The faculty can not be bothered chasing after students to get them to add their Honor Code declaration afterwards.

Programming Projects and Major Assignments: Programming projects and major assignments, such as a term project or an essay (“paper”) must be machine-generated (i.e., not hand-written), and must be submitted both in hard- and in soft-form.

Format for Submission of Programming Projects and Major Assignments: Multiple pages of hard-copy must be stapled together, and both hard and soft copies must have, in the upper left corner of the first page:
(a) your name
(b) course number
(c) section number
(d) semester (e.g., Fall 2001)
(e) date of submission, and
(f) Honor Code declaration, with your signature.

Please note that I have no trouble remembering my own name. Therefore, you do not need to write my name on your homework assignments.

Content of Submitted Work: All written work should be thoroughly professional in accordance with the highest standards. Your writing should be clear, should comply with the rules of grammar of the language in which it is written (for most of our courses, this will be English), as well as with good writing practice, and should be correctly spelled and punctuated and free of both slang and jargon.

Late Submissions Policy: All work is due at the designated date and time. Normally, I do not accept late submission of homework. In order to reduce the need for a student to provide explanations or excuses for not submitting assignments on time or for missing a quiz, I drop the lowest homework grade and the lowest quiz grade.

Grading Policy:

Overall Meaning/Definition of Grades: A grade of A, either on an individual assignment or for the entire semester, indicates work that is truly outstanding in the opinion of the instructor, demonstrating excellent mastery of the material covered. A grade of B indicates very good work, above the instructor’s level of expectation for an undergraduate student. An undergraduate grade of C indicates work that is satisfactory, although not outstanding, demonstrating sufficient comprehension of the material to merit the student’s receiving credit for

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3 If you do not own a stapler, there is one available for student use in the Copy Center (HHS Room 1002).
achieving the course objectives. A grade of \textit{D} indicates work less than satisfactory at the undergraduate level, but nevertheless sufficient to merit receipt of undergraduate credit for the class. A grade of \textit{F} indicates work far below the minimum level considered to be satisfactory, demonstrating insufficient achievement in the skills or level of knowledge required even at the undergraduate level.

\textbf{Extra-Credit Opportunities.} Grades are based only on assignments given to \textit{every} student in the class. Opportunities to earn extra credit may possibly be announced to the entire class at various times during the semester, but extra-credit assignments will NOT be custom-crafted for the sake of an individual student. Your best strategy is to learn the course material by conscientiously studying and doing your assigned homeworks \textit{throughout} the semester. If you wake up near the end of the semester and only then realize that you are in trouble, there may not by then be anything that you can do.

\textbf{Extra Tutorial Assistance:} I will be pleased to provide extra help in most instances to any student who requests it. However, the student who needs help must \textit{both}: \begin{enumerate}[(i)]  
\item take the initiative on his/her own to seek me out, and 
\item seek help in a timely manner and not wait until the last minute, when the examination or assignment due date is already imminent. 
\end{enumerate} You must also understand that I am willing to help when your own assiduous efforts to learn the material prove to be inadequate. I cannot provide tutorial assistance to a student who cannot find the time to do the assigned readings and homeworks, nor for a student who is “too busy” to come to class.

\textbf{Quizzes and Examinations:} There will be one in-semester examination (mid-term), and a final examination. In addition, there will be a relatively brief in-class quiz given approximately \textbf{bi-weekly} throughout most of the semester, except for the week when the Mid-Term Examination is given. The quizzes, as well as the Mid-Term and Final Examinations, will be based \textit{both} upon the reading assignments, \textit{regardless} of whether or not the readings were covered in class, that were due up to and \textit{including} the date of the quiz or examination, \textit{and also} upon the material covered in class up to the moment of the quiz or examination, \textit{regardless} of whether or not the assigned readings also cover the same material. Occasionally a student may have a bad day and will therefore not perform on a quiz up to his/her level of knowledge. Alternatively, circumstances may come up either that prevent him/her from covering the day’s assignment on time, or that preclude his/her attendance on the particular day when a quiz is given. In either case, this will result in a quiz grade below the norm for that student, or in an automatic grade of zero if the quiz is not taken at all, regardless of reason. To avoid excessive anxiety on the part of a student who experiences a rare bad day, and to avoid having to take up students’ and instructor’s time with the giving and adjudication of explanations and excuses, as a matter of policy the lowest \textbf{one} quiz grade for each student will be dropped. Students are warned not to use up their opportunity frivolously (e.g., don’t miss class without grave cause). Preserve your allotment of one excused low quiz grade for circumstances of real need.

\textbf{Homework and Programming Assignments:} There will also be several homework assignments, including one or more programming assignments.

\textbf{Class Participation:} Vigorous student participation in class discussion makes for a much more lively and interesting class for all. To encourage participation in class discussion, the grading mechanism includes the opportunity for the student to earn a reward (details given below) for participating \textit{both vigorously and constructively} in class. Note that your mere attendance can not considered to be “class participation”, and will not be rewarded with class participation points. Attendance in class is \textbf{mandatory}, and therefore you will be given no rewards merely for attendance. However, your vigorous and constructive participation in class discussion will certainly make the class more interesting both for me and for your fellow students as well as for yourself, and this therefore can earn you “class participation points”, which can \textbf{possibly} result in enhancing your grade, as well.

\textbf{Assignment of Grades:} Makeup of overall grade for the semester will be as follows: First, a numeric score will be calculated based upon your performance on all the examinations, and on the quizzes and homeworks.
The basis for calculating your grade for the semester is:

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<table>
<thead>
<tr>
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</thead>
<tbody>
<tr>
<td>Quizzes</td>
<td>20 pts</td>
</tr>
<tr>
<td>Mid-Term Examination</td>
<td>20 pts</td>
</tr>
<tr>
<td>Homework Assignments</td>
<td>30 pts</td>
</tr>
<tr>
<td>Final Examination</td>
<td>30 pts</td>
</tr>
<tr>
<td><strong>TOTAL:</strong></td>
<td><strong>100 pts</strong></td>
</tr>
</tbody>
</table>

Possible extra-credit opportunities to be announced, and participation in class discussion can earn extra points: ≤10 pts

After the numeric scores have been determined, letter grades will be assigned, based upon the distribution of the numeric scores. I make no commitment in advance regarding the letter-grade equivalent of specific numeric grades. The standard cutoff scores for grades are: 90 for A, 80 for B, 70 for C, and 60 for D. However, I reserve the right to lower the cutoff points in accordance with my judgment after studying the actual distribution of numeric scores.

**Enhancement of Grades for Vigorous Class Participation:** An initial assignment of letter grades is made to all members of the class as described above. After making the initial assignment of letter grades, I then dispense additional points to those students, usually few in number, who participated vigorously and effectively in class discussion. This may result in improvement of the grades for such students. Thus, your non-participation in class discussions will not lower your grade, but high-quality participation may possibly raise it.

**Legibility and Clarity-of-Communication Requirements for Quizzes, Examinations, Homeworks, and Term Papers:** It is up to you, the student, to demonstrate to my satisfaction that you have mastered the course material. I know that at the time of your birth you knew nothing about the subject matter of this course. If a change has occurred between then and now, then you must demonstrate through your performance on quizzes and exams that learning has taken place. Therefore, your writing and drawing must be clear and unambiguous, and your answer to each question should be obviously correct on its own, without benefit of any post hoc verbal explanation that you may provide of your answer. What this means is that:

(i) your handwriting must be legible to me;
(ii) you must, yourself, bear the burden of choosing the correct words and technical terms that answer the question;
(iii) your drawings must be neat, technically correct, and properly labeled;
(iv) your sentences must be properly structured, and paragraphs must be correctly and logically organized;
(v) you must thoroughly address all the specific issues raised by the question; and
(vi) for multiple-choice, fill-in-the-blank and other short-answer type questions, you are responsible for marking the answer in the correct place on the answer sheet. The grader will not be responsible for searching for the correct answer in other places, nor can credit be given after the fact for notations made on your question booklet that were not reflected in the answer marked on your answer sheet. Be careful, and check what you are doing. It can be very

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4 Please note that in the unlikely event that the university should close down because of inclement weather or for some other emergency, thus preventing the final examination from being held during the scheduled time, then I shall determine your semester grade based upon the remaining information at my disposal. **There will be no make-up** in this course of the final examination if it cannot be held as scheduled. Please see the “Course Map” for the date and time of the final examination.
frustrating for student and instructor alike when a student who knows the material has to take a lower grade than he or she could have earned, because of the student’s carelessness in marking the answer properly on the answer sheet. Nevertheless, Computer Science, like airline piloting, is notoriously unforgiving of mistakes, and minute attention to detail is one of the personal properties that the faculty tries to inculcate in our students.

Errors in Grading: Unclear answers will be marked **wrong**. Instructors are human and sometimes make mistakes, too. You are entitled to complain politely after class if you honestly feel that your answer is both clear and correct, but was misunderstood at grading time by the instructor. If the instructor agrees that a mistake was made, then your grade will be cheerfully corrected.

Rules for Examinations:

1. **No calculators, no books, no notes.**
2. The JMU Honor Code must be scrupulously observed.
3. All work **must** be shown on your examination paper. You will certainly be given extra paper if you ask for it.
4. You must provide exactly ONE answer to each test question. In the event that you should provide more than one answer, the answer that is **wrong** is the one that will be graded.
5. All examinations **must** be taken at the scheduled time. If you miss the scheduled examination, you are responsible for providing **timely** documentation to support a medical or other **bona fide** emergency to avoid getting a grade of zero for the examination. Medical exemption requires certification from a licensed medical practitioner or facility. The documentation must be provided on the practitioner’s letterhead and must be dated and signed by the practitioner, and must clearly certify the time range over which you were incapacitated. The practitioner’s telephone number must also appear on the document.

**Note** that there is a deadline for submitting your documentation to support medical or other excused absence. The deadline is one calendar week after you return to class.

Homework Assignments:

**Educational Philosophy:** There are three ways for a student to learn complex technical subject matter, such as you will encounter in this course. First is by reading. Second is by coming to class and both watching and listening **interactively.** Third is by working selected problems and examples. This course has been carefully designed to integrate at least the first two, and perhaps all three modes of teaching and learning. There may be some material covered in the reading assignments that will **not** also be covered in the classroom, and there is other material **not** covered in the reading assignments that will be covered **only** in the classroom. Students will be held responsible **both** for the content of all assigned readings, **whether or not covered in class, and also** for all classroom material, **whether or not covered in the assigned readings.** To assist you in reviewing both the readings and the classroom materials, and in preparation for the examinations, review questions covering the main points may be provided, and in some cases answers as well. Students are **well advised** to answer review questions in **writing, and, where applicable, to work out solutions to assigned problems in detail** **before** peeking at the answers. The reason for this recommendation is that in first crafting your own answers or your own solutions you will be much more seriously stress-testing your own level of comprehension of the material. Then, when you
compare your own answers with those provided to you, you will gain much better insight into any deficiencies in comprehension that you may have. If you look at the answers first, it will go much faster for you, but you will suffer in the depth of learning that you will attain. I treat you as adult by providing the answers up front in some cases and by trusting you to use good judgment in working through the problems before consulting the answers. Please don’t disappoint me.

**Types of Assignments:** Details of homework assignments for this course are specified in a separate document. In general, a homework assignment may have one or more of four components: readings, review questions, practical exercises, and reports (oral and/or written). Readings must be done on time, so that you will be properly prepared for, and get full benefit from the class. Review questions are also extremely important for you to answer prior to the class when they are due. In most cases, your answers to review questions will not be collected and graded, but these questions are excellent preparation both for quizzes and for the lengthier Mid-term and final examinations. Readings, review questions, practical exercises, and reports must all be completed no later than the scheduled due date and must be ready for submission on the due date at the beginning of class. Some or all of the homeworks will be collected. These will be graded not on the basis of whether the answers are correct, but merely on the basis of whether the homework was done completely and conscientiously.

**Group Projects:** One or more projects may be assigned during the semester. Any assigned projects, may be assigned either as individual projects or as Group Projects. Any project assigned as a group project must be done as a group project. Even if you prefer to work by yourself and are willing to do by yourself all the work required for the project, you must nevertheless join a group to work on any project designated as a group project, and you must also participate as a full partner with your fellow-students in the group. Group members are advised to exchange both telephone numbers and E-mail addresses immediately upon formation of the group, to facilitate inter-member communication (this is a recommendation, not a requirement). Each member of the group is responsible for cooperating fully with the other members of the group, and for doing his/her full agreed-upon share of the work in concert with the rest of the group. For every group project assignment, the group is required to deliver, along with their written project report, a written *Work Breakdown* statement, indicating precisely what contribution each member of the group made to the overall project.

**Policy Regarding Classes Missed by Students:**

In the university environment, there is an implied contract between students and faculty. You (students) expect us (faculty) to come to class. I, as a faculty member, also expect all of my students to come to class. Occasionally, you may find it necessary to miss a class. If you must miss an occasional class, I trust you, as a responsible adult, to do so only for adequate reason. Therefore, in general you do not need to seek my permission before skipping a solitary class, nor do you need explain afterwards why you were absent. Please note, however, that I do look particularly askance at students who miss the last class prior to a vacation period and/or the first class after vacation. The university is very generous with scheduled vacations, and I expect you to make do with the allotted vacation days and not to take for yourself an extension of your vacation period beyond what the university has generously scheduled for all students and faculty. Airline tickets can usually be procured for travel during the scheduled vacation period, if they are purchased sufficiently in advance. In the event that you are unable to obtain a ticket without committing yourself to straying into the time scheduled for classes, then I invite you to make alternate plans and to spend your vacation closer to Harrisonburg.

If you have missed the class for good and valid reason, nevertheless you are responsible for making up the work you missed, as well as for complying with any announcements, directives, or instructions that might have been
issued during the class that you missed. Therefore, it is up to you both to find out what was covered or announced, and to make up in a timely fashion any missed work.

You would be wise to prepare, as early as the very first day of the semester, for the possible occurrence of sudden brief acute illness (tummy ache, head ache, etc.), or of other, non-medical emergencies, such as a flat tire, traffic jam, family emergency, or the like. I strongly suggest that you exchange phone numbers and E-mail addresses on the first day of class with several of your classmates. If at all possible, give notice to one of your colleagues prior to the class you will miss. Follow up as soon as possible after the missed class, so that you will be able to stay abreast of what is happening in class. Also, if you know in advance that you must miss a class, you should arrange to have someone hand in for you any assignments you may have done that are due that day. If you did not make advance arrangements, then it is even more important both that you follow up rapidly to find out what you missed and that you make up for missed work.

Please do not send me E-mail, either asking in advance of the class you must miss what do I intend to cover, or querying me subsequently to the class on what did I cover. I teach many students each semester, and I just don’t have the time to answer a blizzard of “What will I miss?” and “What did I miss?” E-mails. In the fortunately rare case that a student encounters a serious health problem or a serious issue in his/her personal or family life that spans several consecutive classes, it is my experience that I have almost always been able to make a special accommodation to try to help the student through the crisis, and I will certainly make every effort to do so in the future, as well. But I must insist that you take care of the onesies and twosies on your own.

Class Meetings:

Classes meet during the Spring 2008 semester on Tuesdays and Thursdays from 1100 to 1245 hrs in HHS 2202.

Instructor:

Dr. Charles Abzug  (E-mail: abzugcx@JMU.edu)