

Show that for all integers x and y and all positive integers m :

$$(x + y) \bmod m = \left((x \bmod m) + (y \bmod m) \right) \bmod m$$

and

$$(x \cdot y) \bmod m = \left((x \bmod m) \cdot (y \bmod m) \right) \bmod m$$